Spring Term 2005

## 8.02X Electricity and Magnetism

Quiz#1 Solutions

Tuesday, Feb 22 10:05-10:55am

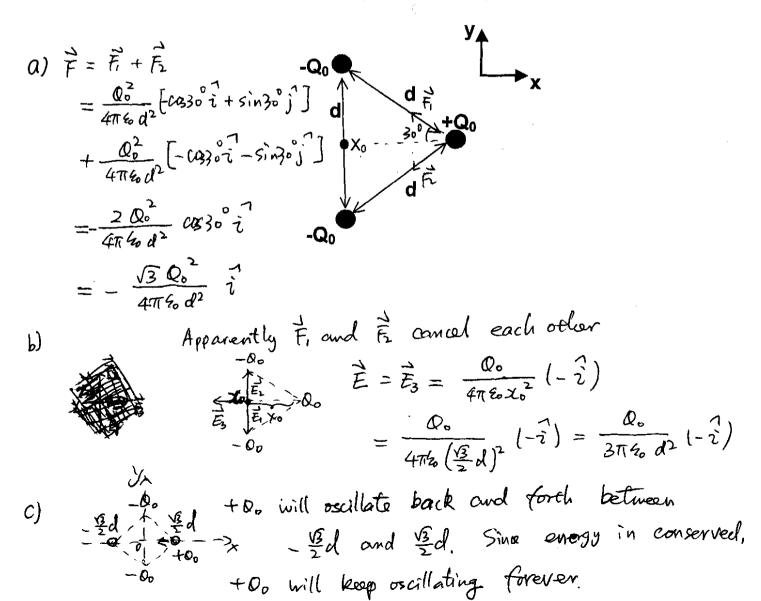
The quiz has four questions. It is a closed book quiz. No calculators are allowed. A letter-size formula sheet can be used, but has to be signed and submitted together with the quiz.

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### Problem 1 (25 points)

Consider the configuration of point charges shown below, with two negative charges  $-Q_0$  and a positive charge  $+Q_0$  forming a equilateral triangle (all sides have length d) in the x-y plane.

- (a) What is the direction and magnitude of the force on the positive charge +Q₀ in terms of the given quantities?
- (b) What is the direction and magnitude of the electric field at point x₀ halfway in between the two negative charges?
- (c) Now, assume that the two negative charges are fixed in space and that  $+Q_0$  is freely movable. Describe the motion  $+Q_0$  would undergo if released from rest from the original position shown below (2-3 sentences)



#### Problem 2 (25 points)

In lecture, you saw that an electrically charged plexiglass rod could be used to attract electrically neutral objects like a balloon made out of conducting foil.

- (a) In a few sentences, explain the origin of the force between a charged object like the rod and an electrically neutral conducting object.
- (b) Attraction can also be seen between a charged object and electrically neutral insulators. For example, the rod can be used to pick up pieces of confetti. How does this differ from the process described in (a)?

On the charged vod and the mobile charge on the charged vod and the mobile charge carriers on the conductor causes charges with the same sign as those on the vod to move to the far side of the concluctor, whereas white charges on the concluctor are altracted and more to the side of the conductor are altracted and more to the side of the conductor also to the vod.

1.e. we get an included dipole. Blo the field created by the vod drops with increasing distance, the attractive force on the near unlike-charges wins over the repulsive force on the far-away like charges, giving a net attractive force between rod and conductor.

This is a similar effect, however the dipole is not induced by a global charge separation across the object, but by polarizing—the t, - negative charges within the molecules making up the charges within the molecules making up the

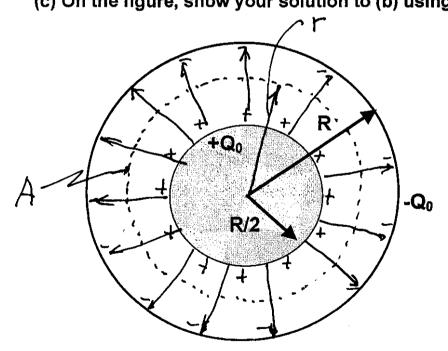
insulator

#### Problem 3 (25 points)

Shown below is the cross-section of a conducting sphere of radius R/2, surrounded by a very thin conducting spherical shell of radius R. The inner sphere carries a charge  $+Q_0$  and the outer shell carries a charge  $-Q_0$ .

- (a) On the figure, indicate the distribution of charge on the inner sphere. + a uniformly distributed on surface y uniformly distributed on surface y
- (b) Using Gauss's Law, find the strength of the electric field E(r) as a function of r from r=0 to r > R, where r is the distance from the center of the sphere. Results without work will not receive credit. O<re>
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 $\frac{R}{L} + \langle R \rangle = \frac{Q_0}{4\pi E_0} + \frac{R}{L}$ (c) On the figure, show your solution to (b) using field lines

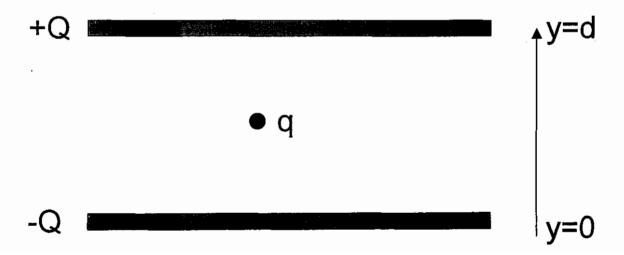


#### Problem 4 (25 points)

Shown below is the cross-section of two large parallel plates carrying charges +Q (top) and -Q (bottom). Each plate has area A. Vertically between the plates, a small charged particle with charge q and mass m is suspended at y=d/2, i.e. the force of gravity  $F_G = -m^*g$  and the electrostatic force on the particle cancel.

- (a) What is the sign of the small particles charge q?
- (b) Determine q in terms of the other quantities given.

  Neglect fringe effects for the electric field created by the two plates.
- (c) Sketch the electric potential energy  $U_E$  of the charged particle as a function of y from y=0 to y=d, assuming  $U_E$  = 0 at y=0.
- (d) Sketch the total potential energy  $U_T$  of the particle as a function of y from y=0 to y=d.
- (e) Sketch the electric potential V between the plates (ignore the charge q) from y=0 to y=d.



# PROBLEM 4

the field is constant between the plates,

with 
$$E = \frac{\sigma}{\epsilon_0} = \frac{Q}{A\epsilon_0}$$

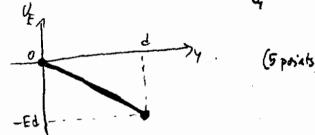
you can get it as a superposition of tields from two infinite plates

a) the change must be attracted to the top plate, so it is negative (2 points)

b) 
$$F_E = F_G \dots Eq = \frac{Q}{AE}q = -mq \dots \boxed{q = -\frac{mq}{Q}\frac{AE}{Q}}$$
 (8 prints)

$$q = -\frac{mq}{Q} \frac{A\xi}{Q}$$

c) the potential energy in a constant field is linear.  $U(y)-U(0)=\int_{-Ed}^{E}q.47=qEy$ Now q is acceptive, so not have  $U(y)-U(0)=\int_{-Ed}^{E}q.47=qEy$ (5 points)

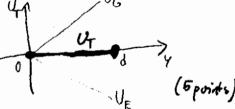


to the potential energy is constant

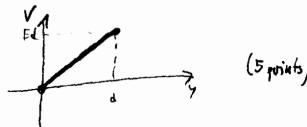
1:1 one ray is constant

(5 points) d) the potential energy lue to gravity is U6 = mgy = (Eq)y ... it is exactly opposite

the total preculial energy is constant



e) the potential between two plates is VW-VIY) = [E.di = -EY ... VCY=VIO)+EY



You can get this also from V= UE (now quas negative, so V has)