

Lecture 1: Using Matlab

- [Using Matlab](#)
 - [Setting Up for Matlab](#)
 - [Basic Calculations](#)
 - [The Matlab “Environment”](#)
 - [Matlab Functions](#)
 - [Matrix Math](#)
 - [Matrix Math](#)
 - [A Motivating Example](#)
 - [Examine the Lift Linkage](#)
 - [Model a System of Forces](#)
 - [Support Forces](#)
 - [Forces on the Bin](#)
 - [System of Equations](#)
 - [What Force for 10lbs Weight?](#)
 - [What about other Weights?](#)
 - [Call the m-file](#)
 - [Expand the m-file](#)
 - [The Matrix Determinant](#)
 - [Plotting Data in Matlab](#)
 - [Matlab plots data, not functions](#)
 - [A Motivating Example](#)
 - [Cool Time Data](#)
 - [Plotting Data](#)
 - [Why an Exponential Look?](#)
 - [Convective Cooling](#)
 - [Curve Fitting](#)
 - [Transform Data to a Linear Form](#)
 - [Plot the Ln Data](#)
 - [Find the Least Squares Fit](#)
 - [Plot both Data and Line](#)
 - [Formatting Plots](#)
 - [Plot the Exponential Equation](#)
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Using Matlab

K. Otto
2.670 ME Tools

Notes:

This is the first day of matlab, and presumes you have sat through the “Introduction to Matlab” training session.

Setting Up for Matlab

```
athena% mkdir ~/matlab  
athena% cd ~/matlab  
athena% add matlab  
athena% matlab &
```

```
athena% mkdir ~/matlab  
athena% cd ~/matlab  
athena% add matlab  
athena% matlab &
```

Notes:

First you need to set up your athena (server) environment to be matlab-happy.

Basic Calculations

```
>> 7+8
```

```
ans =
```

```
15
```

```
>> 7*8
```

```
ans =
```

```
56
```

```
>> 7^8
```

```
ans =
```

```
5764801
```

```
>>
```

```
>> sin(7)
```

```
ans =
```

```
0.6570
```

```
>> sin(7*pi/180)
```

```
ans =
```

```
0.1219
```

```
>> 1/0
```

```
Warning: Divide by zero
```

```
ans =
```

```
Inf
```

```
>>1/0
```

Notes:

Matlab does basic calculations as you would expect.

The Matlab “Environment”

❖ UNIX commands

```
>> ls
.      ..

>> cd ..
>> pwd
/mit/USER

>> cd matlab
>> !lpr FILENAME.ps
```

❖ Workspace commands

```
>> help TOPIC

>> save
>> ls
.      ..      matlab.mat

>> quit

athena% matlab &

>> load

>>
```

Notes:

In matlab, you can do all the UNIX commands.

There is an idea of the matlab workspace. As you define variables and formulas, they are stored, overwritten, expanded, deleted. But there is a state of the matlab environment at any point.

You may choose to leave matlab because of time pressure. You can store the state of matlab with a save command. Then quit matlab, and leave. Later, after starting matlab, just enter load, and the file matlab.mat will be loaded, which restores the state of matlab to what it was when you did the save.

Matlab Functions

- ❖ Consult your *Quick Reference Guide*
- ❖ `help` function provides info
- ❖ 20 Categories of Functions

<code>color</code>	<code>funfun</code>	<code>matfun</code>	<code>sparfun</code>
<code>datafun</code>	<code>general</code>	<code>ops</code>	<code>specfun</code>
<code>demos</code>	<code>graphics</code>	<code>plotxy</code>	<code>specmat</code>
<code>elfun</code>	<code>iofun</code>	<code>plotxyz</code>	<code>sounds</code>
<code>elmat</code>	<code>lang</code>	<code>ployfun</code>	<code>strfun</code>

Notes:

There are many matlab functions..

Matrix Math

Matrix Math

```
>> K = [ 1 0 0 1;
         0 1 0 1;
         0 0 1 1;
         1 1 1 1]

>> det(K)
ans =
    -2

>> K(1:3,2:4)
ans =
     1     0     1
     0     1     1
     1     1     1

>> K*K
ans =
     2     1     1     2
     1     2     1     2
     1     1     2     2
     2     2     2     4

>> Y = K^(-1)
Y =
     0.5    -0.5    -0.5     0.5
    -0.5     0.5    -0.5     0.5
    -0.5    -0.5     0.5     0.5
     0.5     0.5     0.5    -0.5

>> Y*K
ans =
     1     0     0     0
     0     1     0     0
     0     0     1     0
     0     0     0     1

>> d = [ 1 0 0 0 ]
d =
     1     0     0     0

>> f = X*d'
f =
     1
     0
     0
     1
```

Notes:

lets try some matrix math.

A Motivating Example

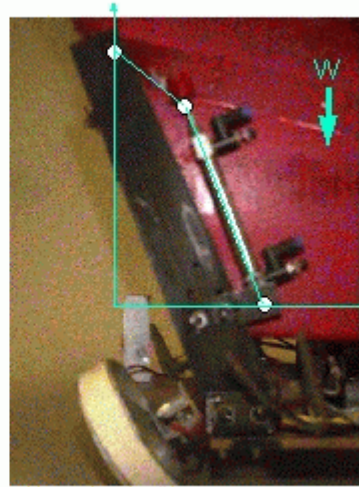
- ❖ 2.007 Contest runner up from a few years ago
- ❖ Drove across a pipe, lifted up a box of balls, and dumped them into a bin

Notes:

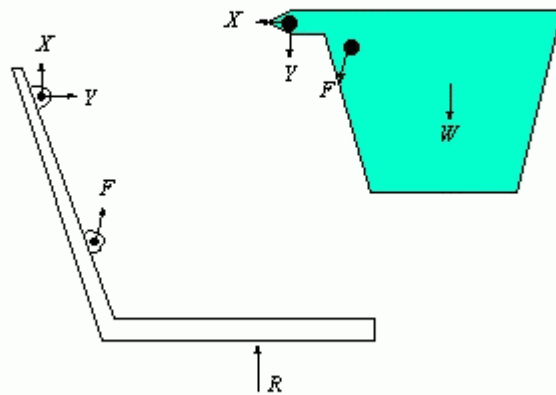
Now lets see how we might use this.

Examine the Lift Linkage

- ❖ How much weight in the bin can the air cylinders lift?
- ❖ An air cylinder can exert ~2 lbs force at 50 psig.



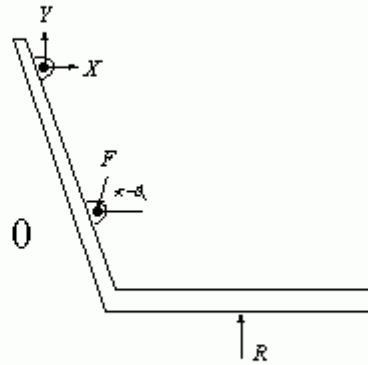
Model a System of Forces



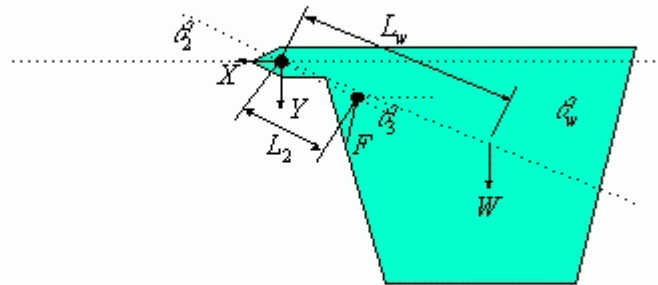
Support Forces

$$Y - F \sin(\pi - \theta_3) + R = 0$$

$$X - F \cos(\pi - \theta_3) = 0$$



Forces on the Bin



$$-Y + F \sin \theta_3 - W = 0$$

$$L_w \cos \theta_w W - L_2 \cos \theta_2 F \sin(\pi - \theta_3) - L_2 \sin \theta_2 F \cos(\pi - \theta_3) = 0$$

System of Equations

This defines a system of equations

$$\begin{bmatrix} 1 & 0 & \cos \theta_3 & 0 \\ 0 & -1 & \sin \theta_3 & 0 \\ 0 & 0 & L_2 \sin(\theta_3 - \theta_2) & 0 \\ 0 & 1 & -\sin \theta_3 & 1 \end{bmatrix} \begin{Bmatrix} X \\ Y \\ F \\ R \end{Bmatrix} = \begin{Bmatrix} 0 \\ W \\ L_w \cos \theta_w W \\ 0 \end{Bmatrix}$$

Or in matrix/vector notation

$$[B]\vec{F} = \vec{R}$$

Note that

$$\theta_2 = 70^\circ \quad L_2 = 1.5''$$

$$\theta_3 = 110^\circ$$

$$\theta_w = 62^\circ \quad L_w = 6.5''$$

What Force for 10lbs Weight?

```
>> rad2 = 70*pi/180;
>> rad3 = 110*pi/180;
>> radw = 62*pi/180;
>> L2 = 1.5;
>> Lw = 6.5;
>> W = 10;
>> Bmat = ...
    [ 1 0 cos(rad3) 0 ;...
      0 -1 sin(rad3) 0 ;...
      0 0 L2*sin(rad3-rad2) 0 ;...
      0 1 -sin(rad3) 1 ];
>> Rvec = ...
    [ 0 ; W ; Lw*cos(radw)*W ; 0 ];
>> Fvec = Bmat^(-1)*Rvec
```

```
Fvec =
    10.8247
    19.7406
    31.6493
    10.0000
```

So the two pistons need a combined force of 32 lbs to lift a bag of sugar in the bin.

What about other Weights?

- ❖ To try many weights, we need an m-file to call many times
- ❖ Call the m-file `force.m`

```
function Fvector = force(W)
% returns the reaction and
% piston forces for a given
% load, at the initial position.
r2 = 70*pi/180;
r3 = 110*pi/180;
rw = 60*pi/180;
L2 = 1.5;
Lw = 6.5;
Bmatrix = ...
    [ 1 0 cos(r3) 0 ;...
      0 -1 sin(r3) 0 ;...
      0 0 L2*sin(r3-r2) 0 ;...
      0 1 -sin(r3) 1 ];
Rvector = ...
    [ 0 ; W ; Lw*cos(rw)*W ; 0 ];
Fvector = Bmatrix^(-1)*Rvector;
```


Call the m-file

```
>> F=force (7)
```

```
F =
```

```
7.5773
```

```
13.8184
```

```
22.1545
```

```
7.0000
```

```
>> F=force (6)
```

```
F =
```

```
6.4948
```

```
11.8444
```

```
18.9896
```

```
6.0000
```

X force on the pin

Y force on the pin

F piston force

R force holding up structure

Expand the m-file

- ❖ Read into the m-file
rad2, rad3, radw
as a vector ang
- ❖ Try
ang(1) = 70*pi/180
ang(2) = 70*pi/180
ang(3) = 62*pi/180
- ❖ What happened?
Why?

```
function Fvector = force(W,ang)
% returns the reaction and
% piston forces for a given
% load W, at a given angular
% position ang = [a1 a2 a3].
r2 = ang(1);
r3 = ang(2);
rw = ang(3);
L2 = 1.5;
Lw = 6.5;
Bmatrix = ...
    [ 1 0 cos(r3) 0 ;...
      0 -1 sin(r3) 0 ;...
      0 0 L2*sin(r3-r2) 0 ;...
      0 1 -sin(r3) 1 ];
Rvector = ...
    [ 0 ; W ; Lw*cos(radw)*W ; 0 ];
Fvector = Bmatrix^(-1)*Rvector;
```

The Matrix Determinant

```
function Fvector = force(W,ang)
r2 = ang(1);
r3 = ang(2);
rw = ang(3);
L2 = 1.5;
Lw = 6.5;
Bmatrix = ...
    [ 1 0 cos(r3) 0 ;...
      0 -1 sin(r3) 0 ;...
      0 0 L2*sin(r3-r2) 0 ;...
      0 1 -sin(r3) 1 ];
disp('The determinant is ');
disp(det(Bmatrix));
Rvector = ...
    [ 0 ; W ; Lw*cos(w)*W ; 0 ];
Fvector = Bmatrix^(-1)*Rvector;
```

```
>> force(10,[70*pi/180,...
            70*pi/180,60*pi/180])
```

The determinant is
0

Warning: Matrix is singular to
working precision.

f =

```
NaN
NaN
NaN
NaN
```

- ❖ B is singular
- ❖ So even infinitely large forces cannot support the bin at these angles.

Plotting Data in Matlab

Matlab plots data, not functions

❖ If you have a vector pair of data, plot it

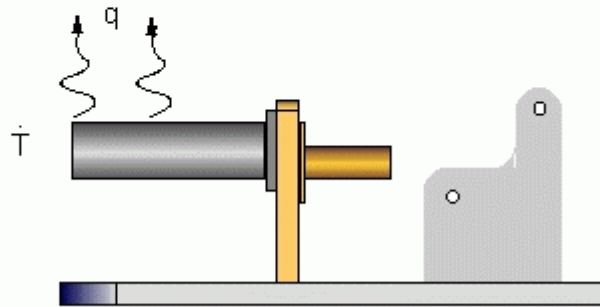
```
>> load('data.dat')  
>> plot(data(:,1), ...  
        data(:,2))
```

❖ If you have a function to plot, first you must generate data that represents it

```
>> Xvec = 0:0.01:4;  
>> Yvec = sin(Xvec);  
>> plot(Xvec, Yvec)
```

A Motivating Example

- ❖ How long until you can grab the machine after blowing out the flame?



Cool Time Data

Measure Temperature at regular time intervals

t (min)	T (F)	t (min)	T (F)	t (min)	T (F)	t (min)	T (F)	t (min)	T (F)	t (min)	T (F)
0.7	859	4.50	248	9.31	154.4	12.29	118.4	17.00	98.2	21.17	87.2
0.99	819.4	4.87	240.2	9.39	152.8	13.00	114.2	17.17	98.2	21.99	87.2
0.50	590	4.39	239.8	9.00	152.8	13.17	119	17.99	98.2	21.50	87.2
0.87	559.4	5.00	230	9.77	149	13.99	111.2	17.50	95	21.87	88
0.99	532.4	5.77	224.8	9.99	147.2	13.50	119	17.87	95	21.99	88
1.00	505.4	5.99	222.2	9.50	145.4	13.87	119	17.99	95	22.00	88
1.77	429.2	5.50	219.2	9.87	149.8	13.99	111.2	18.00	99.2	22.17	88
1.99	480.4	5.87	219.2	9.99	141.2	14.00	109.4	18.17	99.2	22.99	84.2
1.50	430.2	5.99	210.2	10.00	140	14.17	109.4	18.99	99.2	22.50	84.2
1.87	422.8	8.00	208.8	10.17	140	14.99	107.8	18.50	99.2	22.87	84.2
1.99	408.4	8.77	199.4	10.99	150.2	14.50	107.8	18.87	91.4	22.99	84.2
2.00	390.2	8.99	197.8	10.50	154.8	14.87	105.2	18.99	99.2	23.00	84.2
2.77	383.8	8.50	195.2	10.87	158.4	14.99	105.2	19.00	91.4	23.17	84.2
2.99	381.4	8.87	190.4	10.99	154.8	15.00	104	19.17	91.4	23.99	82.4
2.50	350.8	8.99	188.2	11.00	151	15.17	104	19.99	91.4	23.50	82.4
2.87	330	7.00	181.4	11.17	151	15.99	104	19.50	91.4	23.87	82.4
2.99	327.2	7.77	178	11.99	128.8	15.50	102.2	19.87	91.4	23.99	82.4
3.00	318.4	7.99	174.2	11.50	128.8	15.87	102.2	19.99	99.8	24.00	82.4
3.77	307.4	7.50	174.2	11.87	128.8	15.99	100.4	20.00	99.8	24.17	82.4
3.99	302	7.87	172.4	11.99	128.8	18.00	100.4	20.17	99.8	24.99	82.4
3.50	294.2	7.99	168.2	12.00	128.2	18.17	100.4	20.99	87.2	24.50	82.4
3.87	294	8.00	165.2	12.17	128.2	18.99	100.4	20.50	88	24.87	80.8
3.99	275	8.77	160.4	12.99	122	18.50	98.8	20.87	87.2	24.99	80.8
4.00	288	8.99	158	12.50	122	18.87	98.8	20.99	87.2	25.00	80.8
4.77	280.8	8.50	158.2	12.87	120.2	18.99	98.2	21.00	87.2	25.17	80.8

Plotting Data

Copy the temperature data file from the 2.670 locker

```
athena% cp /mit/2.670/Computers/matlab/temp.dat ~/matlab
```

Read data from a file into matlab

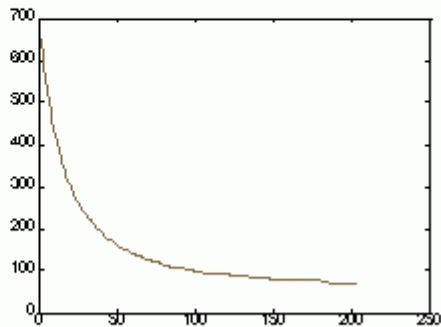
```
>> load('temp.dat');  
>> tvec=temp(:,1);  
>> TmpDatavec=temp(:,2);
```

Now plot the measured data

```
>> plot(tvec,TmpDatavec)
```

Hmmm...

Looks exponential.



Why an Exponential Look?

The plot looks like an exponential decay...

$$\text{Convection Cooling} \Rightarrow q = hA(T(t) - T_\infty)$$

$$\text{Lumped Mass} \Rightarrow -q = mc_p \frac{dT}{dt}$$

$$\frac{dT}{dt} = \frac{-hA}{mc_p} (T(t) - T_\infty)$$

Convective Cooling

Transform variable $D = T - T_\infty$ $\dot{D} = \dot{T}$

$$\text{So } \frac{dD}{dt} = \frac{-hA}{mc_p} D \Rightarrow \frac{-hA}{mc_p} dt = \frac{dD}{D}$$

$$\text{Integrate } \int_0^t \frac{-hA}{mc_p} dt = \int_{D_0}^D \frac{dD}{D} \Rightarrow \frac{-hAt}{mc_p} = \ln\left(\frac{T - T_\infty}{T_0 - T_\infty}\right)$$

So

$$T = T_\infty + (T_0 - T_\infty) e^{\left(\frac{-hA}{mc_p}\right)t}$$

Curve Fitting

- ❖ Matlab only fits polynomials to data....

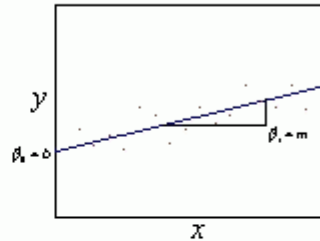
```
>> polyfit(Xvec, Yvec, 1)
```

fits a least squares best line

$$y_{\text{predicted}} = \beta_0 + \beta_1 x$$

to a dataset

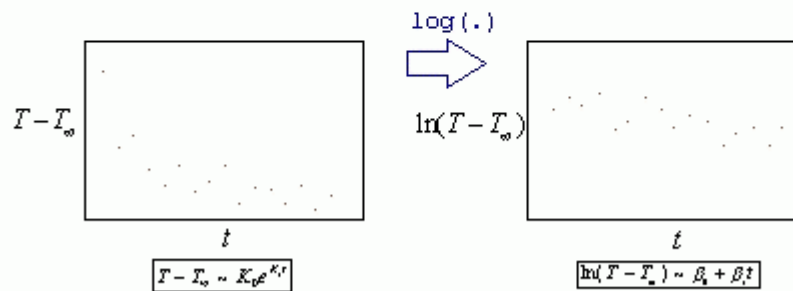
$$\left[\bar{x}, \bar{y}_{\text{measured}} \right]$$



Transform Data to a Linear Form

❖ Our data is exponential, not linear

So take the $\log(\cdot)$ of the data



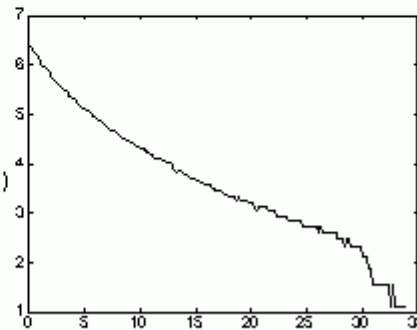
Plot the Ln Data

Just to convince ourselves, lets plot the $\log(\cdot)$ data.

```
>> Tinf = 65;
>> DeltaDatavec = ...
      TmpDatavec - Tinf;
>> lnDeltaDatavec = ...
      log(DeltaDatavec);
>> plot(tvec, lnDeltaDatavec)
```

Ambient Temperature is 65°F

Is it linear?.....



Find the Least Squares Fit

Find the coefficients that least squares best fit a line (a linear polynomial):

```
>> beta=polyfit(tvec,lnDeltaDatavec,1)  
beta =
```

-0.1281 5.7895

A_1

A_0

Which tells us $\ln(T(t) - 65) = 5.8 - .13t$

or $T(t) = 65 + 330e^{-.13t}$

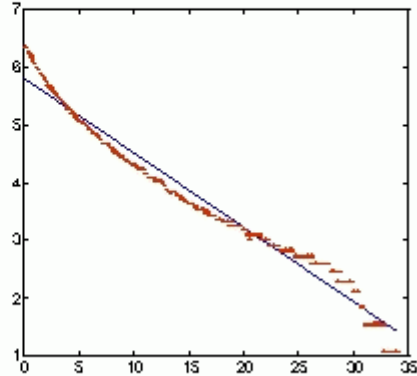
Do you believe this least squares best fit model?

Plot both Data and Line

Lets check by visualizing the data.

```
>> Fitvec = ...  
    beta(1)*tvec ...  
    + beta(2);  
>> plot(tvec,...  
    lnDeltaDatavec,...  
    'r.',...  
    tvec,...  
    Fitvec,'b')
```

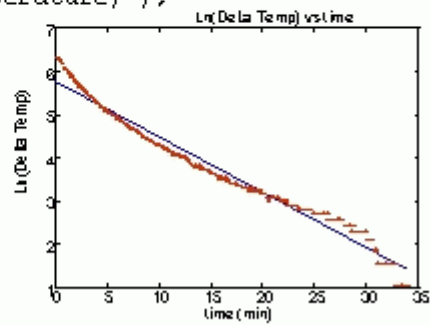
Do you believe the model?



Formatting Plots

Add titles, axis labels, and legends with plot formatting commands

```
>> title('Ln(Delta Temp) vs. time');  
>> xlabel('time (min)');  
>> ylabel('Ln(Delta Temperature)');
```

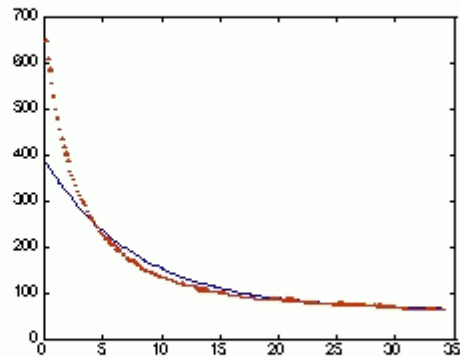


Plot the Exponential Equation

The least squares best fit exponential model to the data is then

$$T = 65 + 330e^{-.13t}$$

How long until we can grab our engine?



Do you believe
- the model?
- the time prediction?