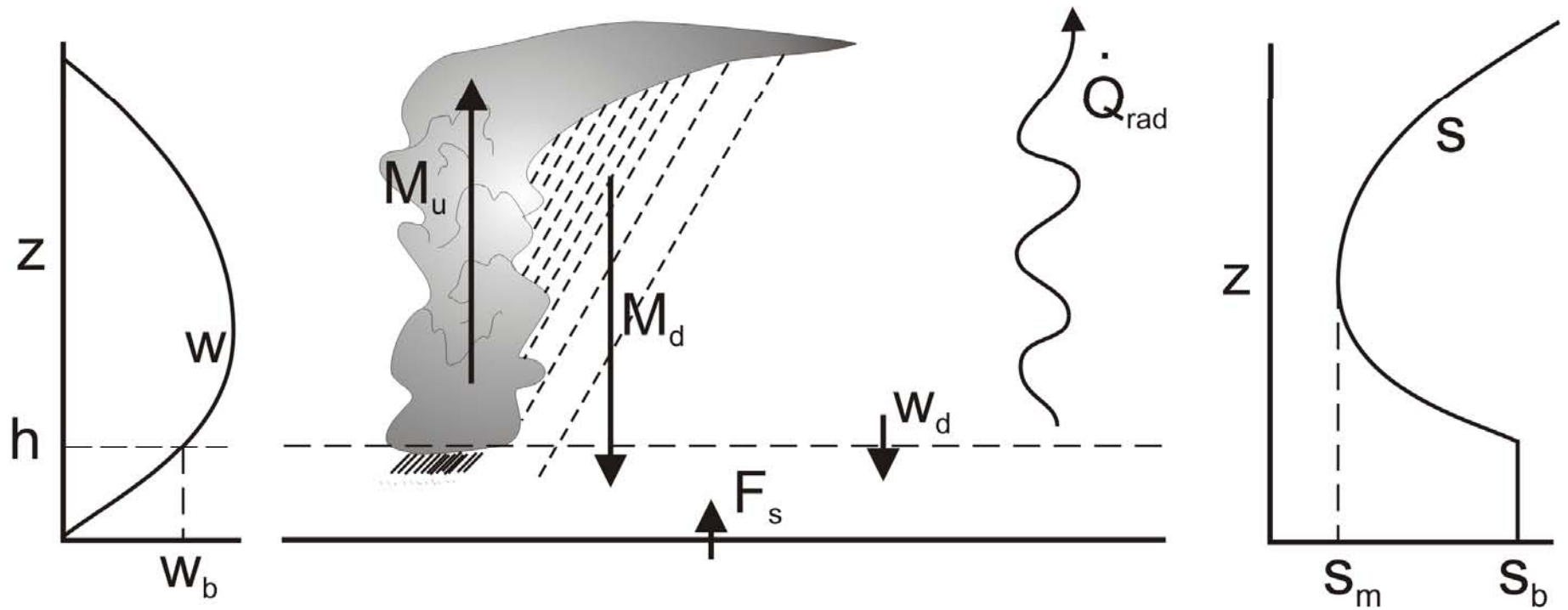


# Relationship between moist convection and Large-Scale flow

Boundary layer entropy equilibrium hypothesis  
(Raymond, 1995)



$$h \frac{\partial s_b}{\partial t} \approx 0 = F_s - (M_d + (1 - \sigma) w_d) (s_b - s_m)$$

Mass:

$$M_u - M_d - (1 - \sigma) w_d = w_b$$

$$\rightarrow M_u = w_b + \frac{F_s}{S_b - S_m} \quad (1)$$

Free troposphere heat balance:

$$(M_u - M_d - w) \mathbf{S} = \dot{Q}_{cool},$$

$$\mathbf{S} \equiv c_p \frac{T}{\theta} \frac{\partial \theta}{\partial z}$$

Convective downdraft:

$$M_d = (1 - \varepsilon_p) M_u$$

$$\rightarrow \boxed{\varepsilon_p M_u = w + \frac{\dot{Q}_{cool}}{\mathbf{S}}} \quad (2)$$

Combine (1) and (2)      *Let*    $w_b = \gamma w$

$$w = \frac{1}{1 - \gamma \varepsilon_p} \left[ \frac{\varepsilon_p F_s}{s_b - s_m} - \frac{\dot{Q}_{cool}}{\mathbf{S}} \right],$$

$$M_u = \frac{1}{1 - \gamma \varepsilon_p} \left[ \frac{F_s}{s_b - s_m} - \frac{\gamma \dot{Q}_{cool}}{\mathbf{S}} \right]$$

Note that       $M_u > w$

Radiative-convective equilibrium:  $w=0$

$$\rightarrow F_s = \frac{\dot{Q}_{cool} (s_b - s_m)}{\mathbf{S} \varepsilon_p},$$

$$M_u = \frac{\dot{Q}_{cool}}{\mathbf{S} \varepsilon_p}.$$

Define

$$(F_s)_{eq} \equiv \frac{\dot{Q}_{cool} (s_b - s_m)}{\mathbf{S} \varepsilon_p}$$

Then

$$w = \frac{\varepsilon_p}{1 - \gamma \varepsilon_p} \left[ \frac{F_s}{s_b - s_m} - \frac{(F_s)_{eq}}{(s_b - s_m)_{eq}} \right]$$

Surface fluxes:  $F_s \cong C_k |\mathbf{V}| (s_0^* - s_b)$

$w > 0$  if

- $F_s > F_{eq}$
- $(s_b - s_m) < (s_b - s_m)_{eq}$
- $Q_{cool} < (Q_{cool})_{eq}$

Note also that we must have  $M_u \geq 0$  so

in circumstances under which (1) and (2) yield  $M_u < 0$

we take  $M_u = 0$ ,

$$w_b = - \frac{F_s}{s_b - s_m} \quad \text{or} \quad s_b - s_m = - \frac{F_s}{w_b}$$

$$w = - \frac{\dot{Q}_{cool}}{S}$$

radiative-subsidence balance

# Weak Temperature Gradient Approximation (WTG) Sobel and Bretherton, 2000

- Ignore time dependence of  $T$  above PBL
- Determine  $w$  from aforementioned equations
- Determine vorticity from  $w$
- Determine  $T$  by inverting balanced flow



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