

4/97  
3/98  
4/01

# Strength-Deformation Behavior of Saturated Clays and Drained/Undrained Stability (Parts D & E of Outline)

## I STABILITY PROBLEMS AND DRAINED STRENGTH PARAMETERS

Handout Sheets

### A. Classes of Stability Problems & Types of Stability Analyses

IA, 2

Review of 1.361 Part V-3

### B. Determination of Effective Stress Failure Envelopes for CD Case

IB

#### 1. Use of CD & CU Tests

1, 2

- 1) CD DS    2) CD TX    3) CU TX

#### 2. Miscellaneous

- 1) Variation in ESE: OCR=1  
2) " " " : High OCR  
3) Common travel testing problems  
4) Comparison of ESE and correlations

3

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4-6

### C. Long Term (CD Case) Stability: Problem Soils

IC

#### C.1 Stiff Fissured and Stratified Clays & Clay Shales

- 1) Introduction  
2) Definition of 3 envelopes (peak, fully softened & residual)  
3) Measurement of residual envelope  
4) Overview of fully softened vs residual envelopes  
5, 6, 7) Recommendations for selecting  $c'$  &  $\phi'$  as per  $\approx 1995$   
and results from recent research  
8) Basic research on  $\phi'$   
9) Empirical correlations

1

2

3

4

4-7

8, 9

8, 10, 11

#### C.2 Highly Structured, Sensitive Clays (Quick Clays)

- 1) Background  
2) Norway  
3) Quebec

12

12

12, 13

#### C.3 Conn. Valley Varved Clays

14

## Mini-Problem No.1 on Strength of Clays

| Topic in HO Notes                      | Approx Date | Questions   |
|--|-------------|---|
| IB<br>Measurement<br>of $c'$ & $\phi'$ | 4/4/01      | 1) What can cause major errors in the measurement of $c'$ & $\phi'$ for CD analyses of <u>homogeneous</u> cohesive soils?   |
| IC<br>Problem<br>Soils                 | 4/4/01      | 1) For cuts in stiff fissured & stratified soils <ol style="list-style-type: none"> <li>When safe to use peak envelope?</li> <li>" " " " NC " ?</li> <li>When must use <math>\phi'_r</math>?</li> <li>When get combination of above?</li> </ol> } Are these 3 envelopes curved? ( $\sigma'_{ff} = 50-400 \text{ kPa}$ )?<br>2) What is effect of using undisturbed or remolded clay on value of $\phi'_r$ ?<br>3) For cuts on natural slopes in quick clays, is CD ESA w/ equilibrium $u$ & peak ESE safe?  |
| II A<br>$s_u$ for<br>UU Case           | 4/9/01      | 1) FVT <ol style="list-style-type: none"> <li>Why does <math>\mu</math> decrease with increasing PE?</li> <li>What soils <math>\rightarrow</math> unsafe to use <math>\mu</math>?</li> </ol> 2) CPTU <ol style="list-style-type: none"> <li>How is <math>N_k</math> determined?</li> <li>What is the major cause of problem in getting consistent <math>q_t</math> profiles in soft clays?</li> </ol> 3) DMT: How reliable is $s_u/\sigma'_{vo} = 0.22(\text{OCR})^{0.8}$ where $\text{OCR} = (0.5k_p)^{1.56}$ ?<br>4) When would you replace unconf. compression test with a UUC test ( $\sigma_c = \sigma_{vo}$ )?<br>5) Did Bishop & Bjerrum (1960) conclude that both UUC & $s_u(FV)$ + reliable $s_u$ for UU Case? |

CCL 3/29/01

1.322

## Class Schedule & Reading Assignments: STABILITY & STRENGTH OF COHESIVE SOILS

○ = STUDY

| Topics  | Handout Notes | '77 SOA Tokyo | '85 SOA SF. | CCL '91 TL | Other                    | Comments (x No. Classes)  |
|---|---------------|---------------|-------------|------------|--------------------------|---|
| 1) Stability Classes & Types of Analysis                      | IA            |               |             | 1, ②       | 1.361<br>IV3-152         | (2+)  |
| 2) CD Case<br>• Measurement $c'$ & $\phi'$<br>• Problem Solv. | IB<br>IC      |               |             |            |                          |   |
| 3) UU Case: Std Practice & In Situ Testing                    | IIA           | 4.2           | 3.2, 3.3    | 4, 6       | 1.361<br>IV4-152         | (1-)  |
| 4) Sample Disturbance   | IIB           | 2.2.7         | ②.3         | ④          | above                    | (2) <span style="font-size: 2em;">}</span> Done HP#4 Q&A MTE 4/18 |
| 5) Stress System & Anisotropy<br>(Combined old & new notes)   | IIC           | 2.2.2         | 2.4         | ④          | -                        | (4+)  |
| 6) Time Effects: Strain Rate & Creep                          | IID           | 2.2.6         | -           | -          | -                        | (2+)  |
| 7) CU Case  | IIE           | -             | -           | ③, 5 & 6   | Koutsofias & Ladd (1985) | (1)   |
| 8) Home Problem or Design Discussion                          |               |               |             |            |                          | (1)   |

NOTE: There will be a series of mini-problems, mostly in the form of questions for class discussion on Topics 1 → 7. Topic 7 will have a major design problem.



4/97  
3/98  
4/01

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4) Comparison of ESE and correlations

4-6

C. Long Term (CD Case) Stability: Problem Soils

IC

4/2/01

CHARLES C. LADD

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3,4

3,5,6

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Wed 4/4/01 since

rewriting - updating not

yet finished

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22-141 50 SHEETS  
22-142 100 SHEETS  
22-144 200 SHEETS

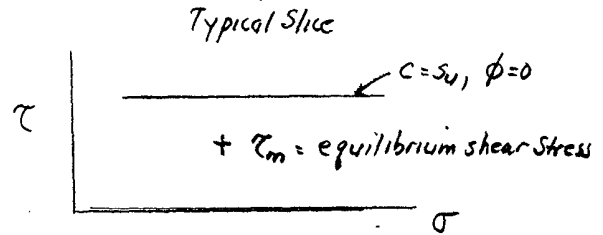
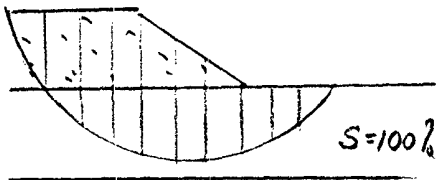


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IA: CLASSES OF STABILITY PROBLEMS AND TYPES OF STABILITY ANALYSES (Sheet A2; Table 6)

CASE 1 = UU Case (Undrained)

Embankment on Soft Clay



Conventional Practice to Est.  $s_u$   
 In Situ FVT CPT etc  
 Lab UUC LV TV etc.

Also BC  $q_{ult} = cN_c + \frac{1}{2} \gamma B N_q + \gamma d N_q$

TSA = Total Stress Analysis

NOTE: Also can/should use USA

CASE 2 = CD Case (Fully Drained)

- Slow const. or long time  $\rightarrow u_e = 0$
- Slow failure  $\rightarrow u_s = 0$

ESA = Effective Stress Analysis (Drained Strength Analysis)

Sheet A2, Fig. 1

For same FS on  $c'$  &  $\phi'$   $\rightarrow$

$FS = \tan \phi' / \tan \phi'_m$

Next: Testing  $\rightarrow c' \& \phi'$   
 (IB)

CASE 3 = CU Case (Partial drainage prior to Undrained Failure)

- $u_e \geq 0$
- $u_s > 0$

Sheet A2, Fig. 3

USA = Undrained Strength Analysis

$c_u = f(\sigma'_{ve}, \sigma'_p)$

CCL Methodology - Use  $CK\&U$

QRS " " UU/CU (Sheet A2, Fig. 2)

CRITICAL CONDITIONS (à la 1.361)

Loading (Construction  $\rightarrow +\Delta P$ )

- Footings, tanks, emb, dams ...
- UU critical since  $+u_e$   
 $\uparrow$  drainage  $\rightarrow$  incr. str.  
 (esp. low OCR)

Unloading (Construction  $\rightarrow -\Delta P$ )

- Excavations, etc
- CD critical since  $-u_e$   
 $\uparrow$  drainage  $\rightarrow$  decr. str.  
 (esp. high OCR with  $-u_s$ )

TABLE 6. Stability Problems Classified According to Drainage Conditions and Definition of Factor of Safety

| Case (1) | Common description (2)                       | Proposed description (3)  | Proposed classification (4)        | Definition of factor of safety <sup>a</sup> (5) |
|----------|--|---|------------------------------------|---|
| 1        | Undrained, short-term or end-of-construction | No consolidation of soil with respect to applied stresses and undrained failure               | Unconsolidated-undrained = UU case | $s_u/r_u$ or $c_u/r_u$ (Eq. 5 or Eq. 8)         |
| 2        | Drained or long-term                         | Full consolidation of soil with respect to applied stresses and drained failure ( $u_r = 0$ ) | Consolidated-drained = CD case     | $s_d/r_m = \tan \phi' / \tan \phi_m$ (Eq. 7)    |
| 3        | Partially drained or intermediate            | Partial or full consolidation of soil with respect to applied stresses and undrained failure  | Consolidated-undrained = CU case   | $c_u/r_u$ (Eq. 8)                               |

<sup>a</sup> $r_u$  = mobilized shear stress required for equilibrium;  $s_u$  = undrained shear strength obtained from conventional testing associated with typical  $\phi = 0$  analyses;  $c_u$  = undrained shear strength obtained from techniques recommended in Section 5; and  $s_d$  = drained shear strength defined in Eq. 1.

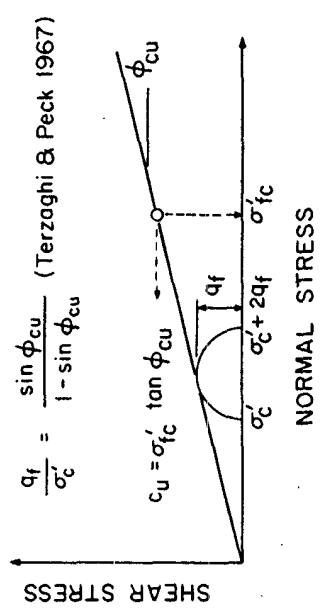
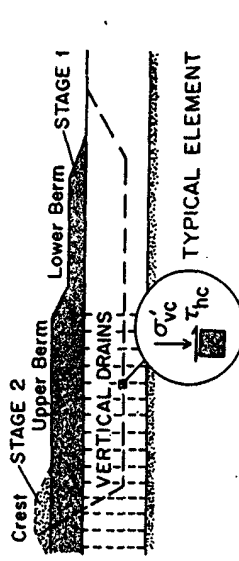


FIG. 2. Angle of Shearing Resistance  $\phi_{cu}$  from Isotropically Consolidated-Undrained Triaxial Compression (CIUC) Tests as Defined by A. Casagrande

(a) FIELD SITUATION FOR PARTIALLY OR FULLY CONSOLIDATED CLAY FOUNDATION



(b) STRENGTHS PREDICTED FROM ESA AND USA

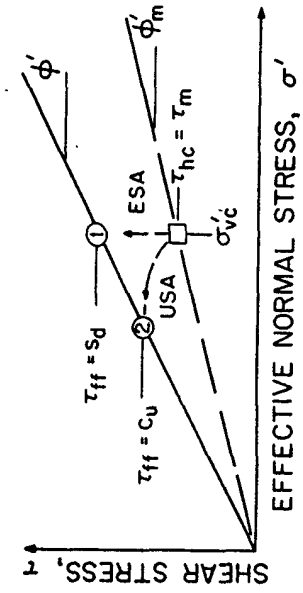
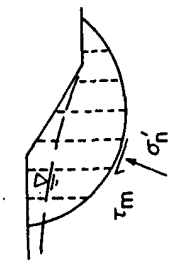
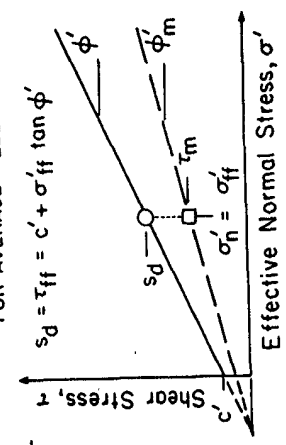


FIG. 3. Comparison of Effective Stress and Undrained Strength Analyses for Evaluating Stability during Staged Construction

(a) EXCAVATION IN STIFF CLAY



(b) STRESSES AND SHEAR STRENGTH FOR AVERAGE ELEMENT



(c) DEFINITION OF FACTOR OF SAFETY (Bishop 1955; Janbu 1973)

$$FS = \frac{s_d}{\tau_m} = \frac{\tau_{ff}}{\tau_m} = \frac{\tan \phi'}{\tan \phi_m}$$

FIG. 1. Conventional Effective Stress Analysis Applied to Critical CD Case for Unloading Problem

4/2/96

IB DETERMINATION OF EFFECTIVE STRESS FAILURE ENVELOPE FOR CD CASE (Saturated Natural Cohesive Soils)

1. USE OF CD & CU TESTS

Note: Limited data on "ordinary" clays indicates that  $t_f$  has little effect on values of  $c'$  &  $\phi'$  (i.e., using  $t_f > t_{100}$  required obtain  $u_s = 0$ )

1.1 CD Direct (Box) Shear Tests

a) Advantages

- Simple equipment & easy to run
- Low cost
- Short  $t \leq 1$  day

b) Disadvantages

1) Non-uniform stress-strain condition  $\rightarrow$  no  $\tau$  vs  $\sigma'$  data.

2) Unknown stress condition at failure

(a)  $\tau_h = \tau_{ff}$ ;  $\delta = 45 + \phi'/2$ ;  $\tau_h/\sigma'_v = \tan \phi'$

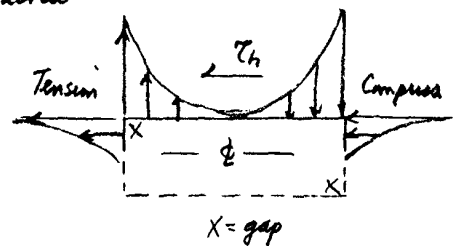
(b)  $\tau_h = |q_c|$ ;  $\delta = 45^\circ$ ;  $\tau_h/\sigma'_v = \sin \phi'$

$\tau_h/\sigma'_v = 0.5 \rightarrow \phi' = 26.6^\circ$  (a)  
 $= 30.0^\circ$  (b)

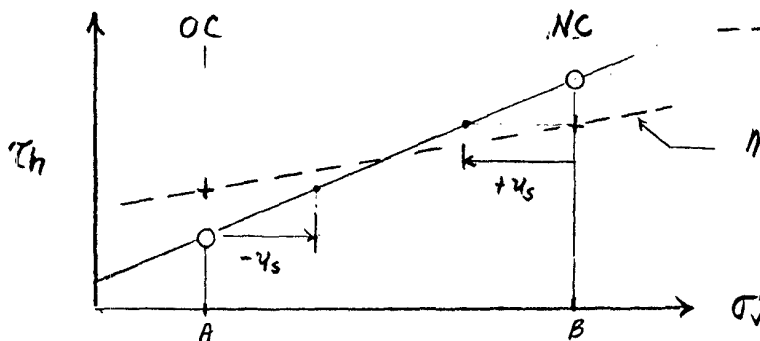
Std. practice

3) Tilting at high  $\tau_h/\sigma'_v$

- Tensile  $\sigma$  at leading portion
- Compressive  $\sigma$  at trailing portion



4) Run test too fast ( $t_f \ll \approx 10 t_{100}$ )



—○— Drained,  $u_s = 0$   
 - - - + - - Too fast,  $u_s \neq 0$   
 (HAND CRANKED)

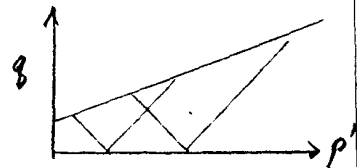
Measured  $c'$  too high  $\rightarrow$  unsafe FS for shallow slope failure

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1.2 CD Triaxial (Usually CIDC L/U since  $K_e$  does not affect  $c'$  &  $\phi'$ )

a) Advantages

- Know stress conditions and meaningful shear-strain data
- Can vary ESP to define ESE at low stresses
- ∴ most reliable



b) Disadvantages

- More complex equipment & harder to run
- Much longer time (1-2 weeks) & more expensive

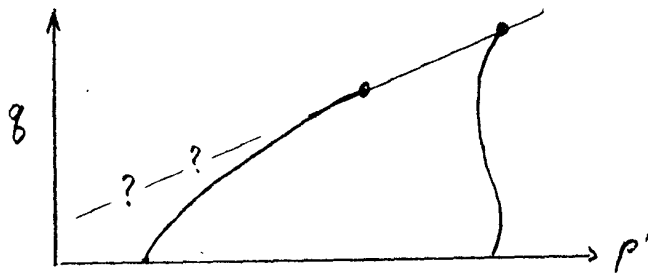
1.3 CU Triaxial (Usually CIUC)

a) Advantages

- Obtain information on undrained behavior for CU Case
- Less time than CIDC

b) Disadvantages

- 1) Procedures more complex to ensure reliable  $\sigma_1$  &  $\sigma_3$  data
- 2) Cannot define ESE at low  $\sigma_1$  for high OC soils



(plus have curved ESE, see p IB6)

3) Varying ESE at  $q_f$ , max obl. & tangency (See 2.1 & 2.2)

Note: generally use max obl. or tangency to estimate  $c'$  &  $\phi'$  for CD Case

4) Potential large unsafe error in  $c'$  if do not obtain pore pressure equalization (See 2.3)

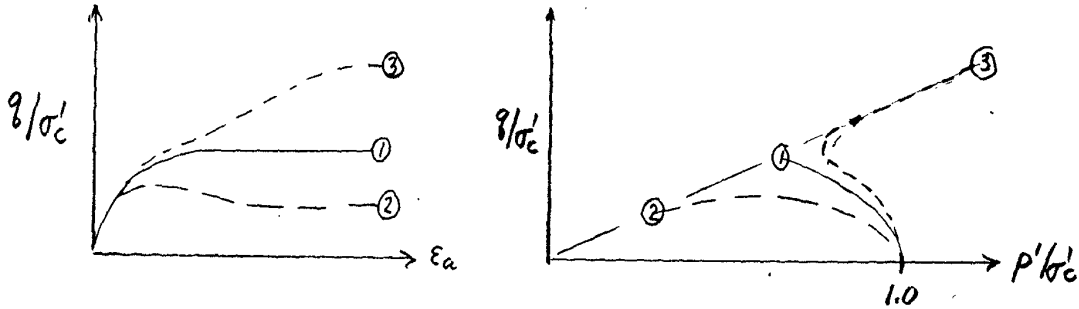


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2. MISCELLANEOUS

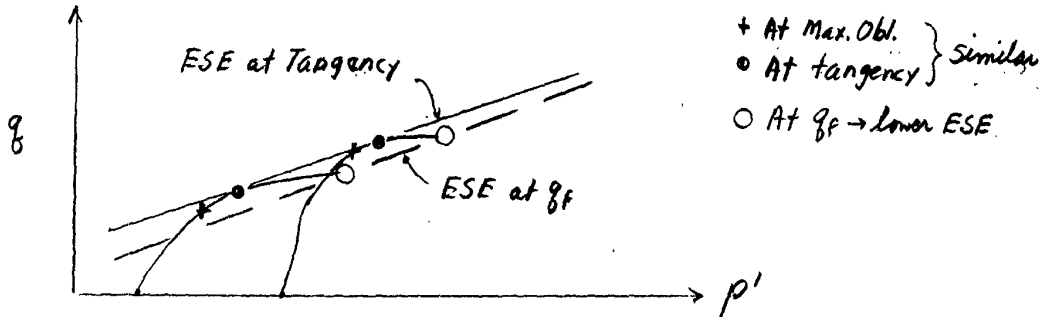
2.1 Variation in ESE : OCR=1 (CIUC Tests)

- ① Simple clay type behavior :  $\phi'_{ff} = \phi'_{mo}$
- ② Sensitive clay ;  $\phi'_{ff} < \phi'_{mo}$
- ③ Archie silt : not really NC  
Cohesionless (small  $\phi'$ )



- Value of  $q = f(\text{mobilized } \phi') \times (\text{magnit. of } p')$  ; High  $S_t$ ,  $\phi'_{ff} < \phi'_{mo}$  by 5-10°  
 In. of  $\epsilon_a$       Dec. of  $\epsilon_a$
- CDC  $\phi'(q_f = mo) \approx$  CIUC  $\phi'_{mo} - (0-3^\circ)$

2.2 Variation in ESE : High OCR (CIUC Tests)

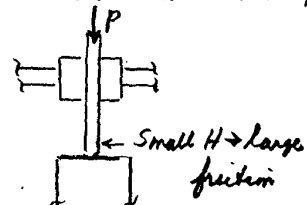


- Usually select ESE at Max. Obl. or tangency to estimate ESE for CD Case  
 But extrapolated envelope is TOO HIGH at low  $p'_f$  (See IB6)

2.3 Common Triaxial Testing Problems (Jermami & Ladd, 1988 ASTM STP 97) +1.37

a) Piston Friction (CU/CD)

- Need ball bearing-rolling diaphragm or internal load cell for reliable  $\sigma_1 - \sigma_3$
- Solid bushing liable  $\rightarrow$  serious errors

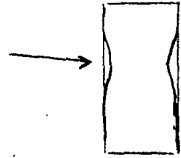


b) Filter strips (CU & CD)

- Compression:  $10\text{cm}^2 \times 8\text{cm}$  Typical correction  $Dq \approx 100\text{pst} = 5\text{kPa}$
- Extension: Need spiral + pre-cut notches  $\rightarrow$  maximum flexibility

c) Area Correction (CU & CD)

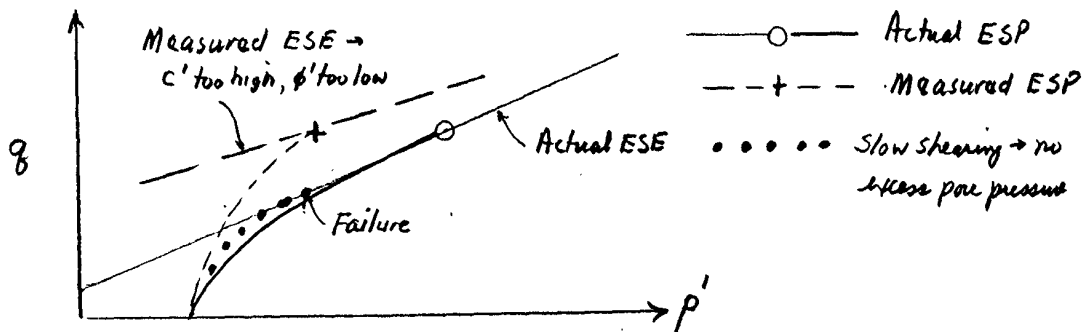
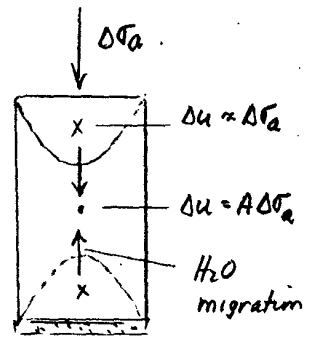
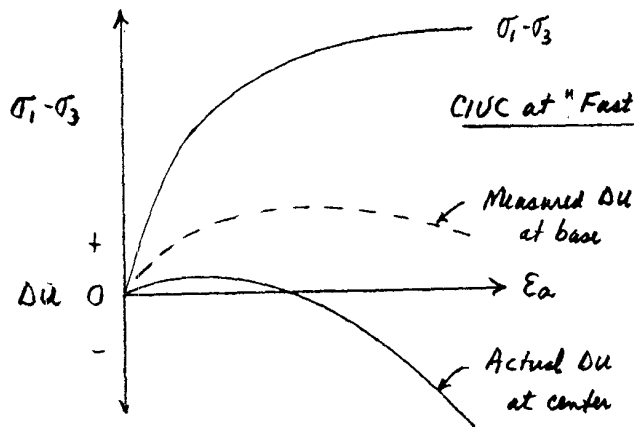
- Compression: See G & L (88) for cylinder, parabolic & bulging
- Extension: Discard data when noticeable necking occurs



d) Saturation (CU)

- Need min.  $u_b \approx 2-3\text{ atm}$  • Always check that  $B \geq 95\%$  few minutes

e) Fractional Ends - Pore Pressure Equilibration at "High" OCR (CIUC)



Correct ESE requires: 1) Either  $u$  measured at  $\frac{L}{2}$  if fast (+ correct  $u_b$ ) (with fractional ends) 2) Or very slow if  $u$  measured at base ( $u_b$  too low)

## 2.4 Comparison of ESE and Correlations

a) Natural BBC :  $CK_0UC/E$  ;  $OCR=1.5-6$  ; Max. Obl. (CAIT Project)

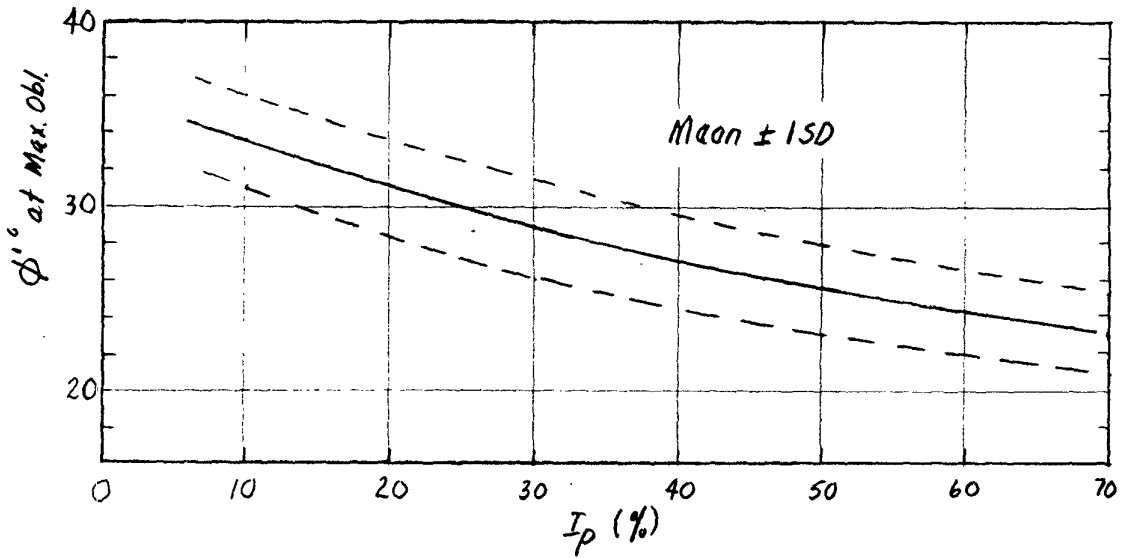
|    | SIHANSEP          |         | Recompression  |         |
|----|-------------------|---------|----------------|---------|
|    | $c'/\sigma'_{vm}$ | $\phi'$ | $c'/\sigma'_p$ | $\phi'$ |
| TC | 0.017             | 28.5    | 0.044          | 29      |
| TE | 0.055             | 19      | 0.031          | 27      |

Large difference  
TC vs TE
Similar values  
TC vs TE

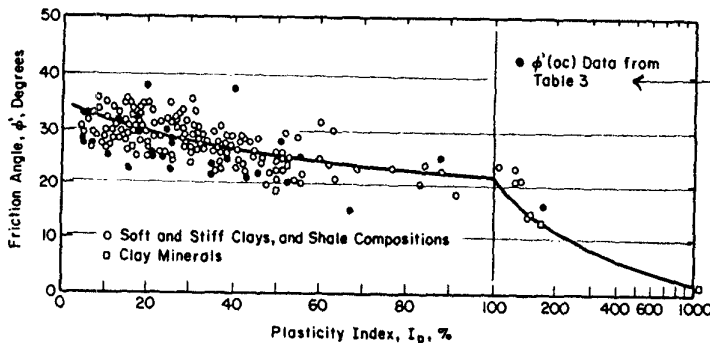
NOTE: Will discuss difference between TC vs TE more fully under IIC

b) Friction Angle vs. Plasticity Index : Normally Consolidated Soils

1) NAVDOCKS DM-7 (1961)



2) Mesri & Abdel-Ghaffar (1993) JGE, ASCE, 119(8), 1516-1249



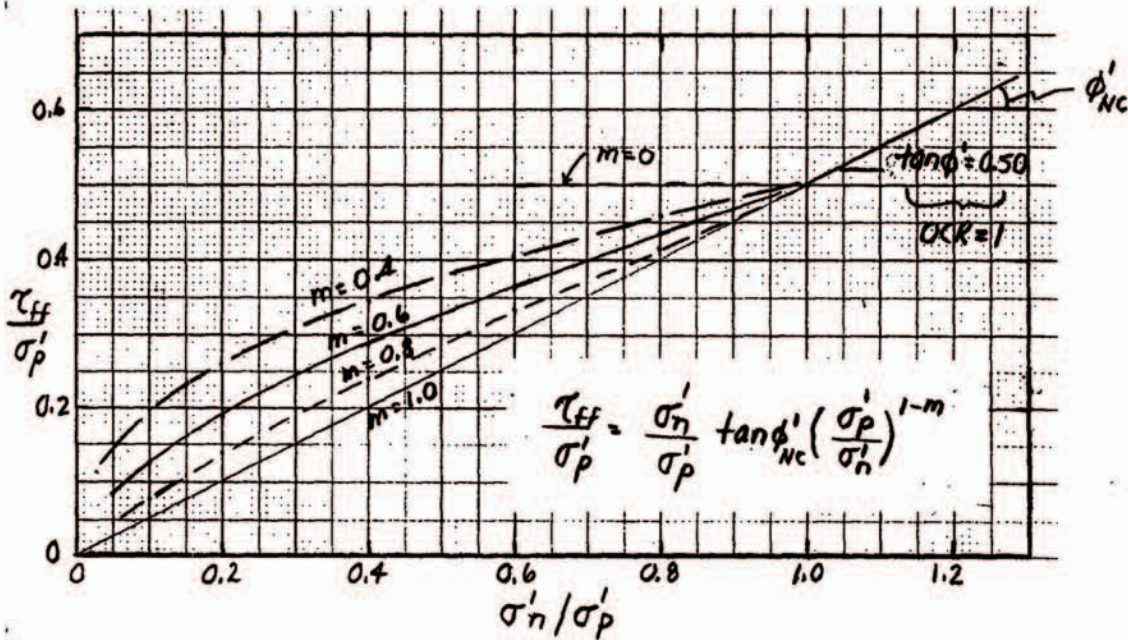
$\phi'$  for OC clay

Data mostly from:  
CIUC  
CIDC  
CDDS

FIG. 2. Values of Friction Angle  $\phi'$  for Natural Clay Compositions

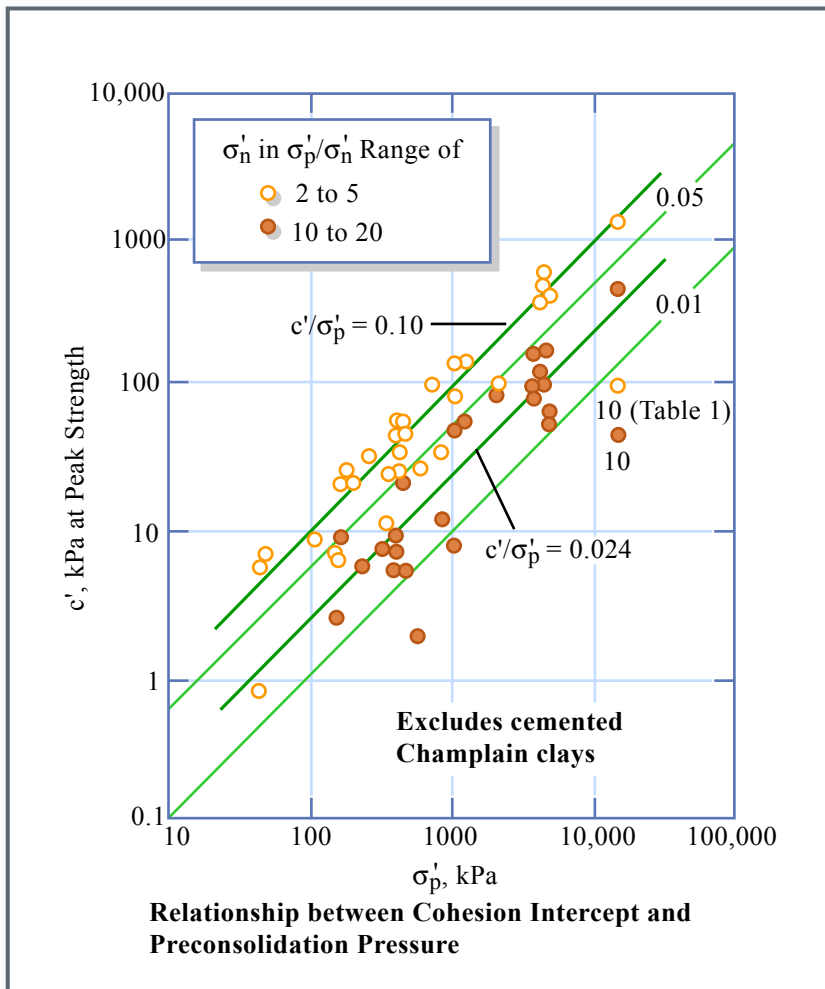
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3/25/99

c) Magnitude of  $c'/\sigma'_p$  from Mesri & Abdel-Ghaffar (1993)



• Shows increasing curvature of ESE as function of  $m = d \log \tau_{eff} / d \log \sigma'_n$  for  $\sigma'_n \leq \sigma'_p$

} Note: Fig. 8 of paper shows  $m = 0.83 - 0.9 I_p$  for  $I_p > 20 - 80\%$



CCL Conclusion For Mechanically OC Clays:

| $\sigma'_n/\sigma'_p$ | $c'/\sigma'_p$ |
|-----------------------|----------------|
| ○ 0.2-0.5             | 0.05-0.1       |
| ● 0.05-0.1            | 0.03±0.02      |

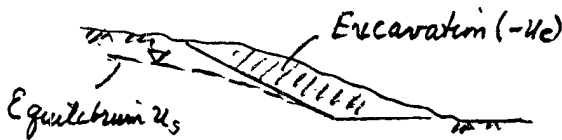
Figure by MIT OCW.

LONG TERM (CD) STABILITY: PROBLEM SOILS

C1 STIFF FISSURED & STRATIFIED CLAYS AND CLAY SHALES

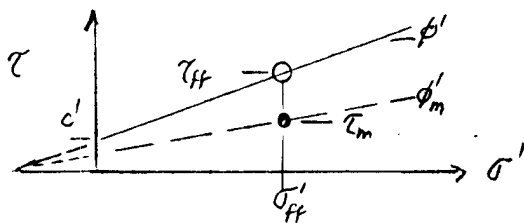
1.1 Introduction

1) Critical condition



$$s_d = \tau_{ff} = c' + (\sigma - u_s) \tan \phi'$$

$$FS = \frac{s_d}{\tau_m} = \frac{\tan \phi'}{\tan \phi'_m}$$



2) Values of  $c'$  &  $\phi'$  to use in analysis depend on:

- a) 1st time vs prior (reactivated) slide.
- b) Homogeneous (also probably low PI & CF = clay fraction)  
vs. Non-homogeneous (NH) stiff clay & clay shales that contain:

- (1) Fissures = small, random oriented discontinuities (like closed cracks; some may be slickensided = "polished")
  - (2) Bedding planes - laminations: These are especially important if more plastic than "bulk" soil and have a higher in situ degree of parallel particle orientation
- Stratified — {

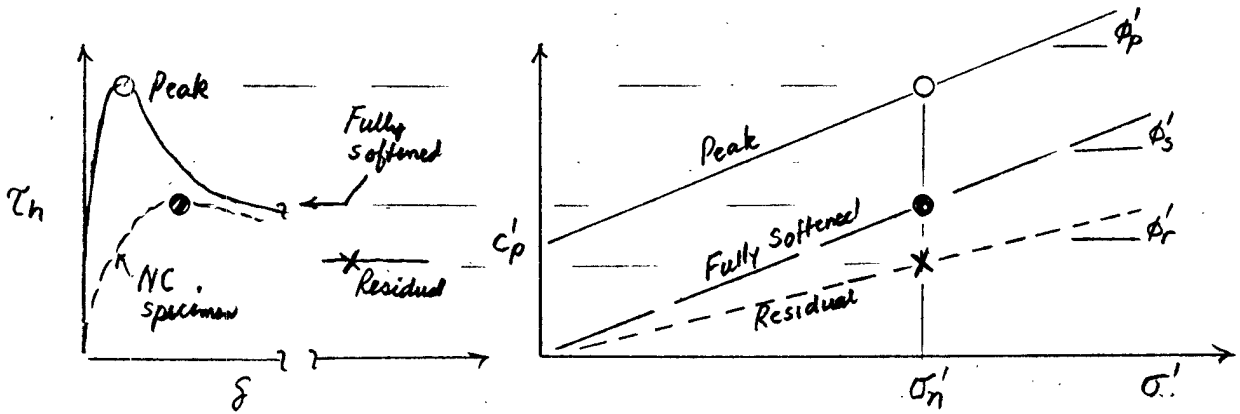
NOTE: NH can have either or both (plus other features such as joints and faults, although these more typically associated with rock).

3) To appreciate problem with selection of  $c'$  &  $\phi'$ , need to understand differential in  $\tau$  &  $\sigma$  as function of degree of shearing



1.2 Definition of 3 Envelopes (e.g. Skempton 1964, Geot. 14(1), 77-108)

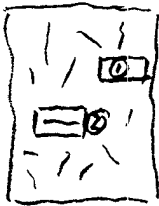
Results from CD DS tests on stiff, fissured London Clay (LL=80, PI=50, CF=55)



1) Peak Envelope ( $c'_p$  &  $\phi'_p$ )

- Magnitude = function of size of specimen if fissured = parallel & inclined to stratification

• Example for stiff, London Clay (Skempton & Hutchinson 1969, ICSEME)



① Intact  $c'_p = 1500 \text{ pst}$   $\phi'_p = 28^\circ$

② Along fissure  $c'_p = 140$   $\phi'_p = 18.5^\circ$

2) Residual ( $\phi'_r$ ) [Note: We'll later see that actually curved]

- Shear to very large displacements leading to maximum orientation of platy particles.
- If  $CF > 50\%$  & high PI, get smooth "polished" surface

3) Fully Softened ( $\phi'_s$ ) [Note: also may be curved]

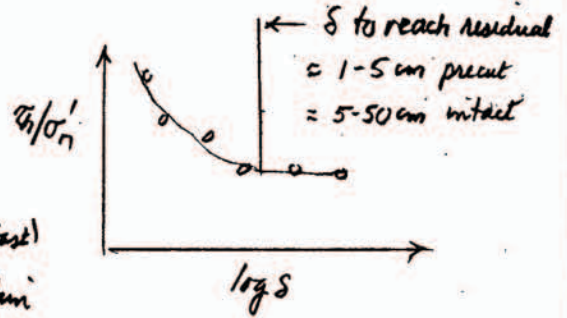
- Corresponds to "critical state", i.e. peak strength from shearing OCR=1 specimen = steady state strength of OC specimens
- Skempton also postulated that have "minor shears not yet linked into a continuous surface" at fully softened state



### 1.3 Measurement of Residual Envelope

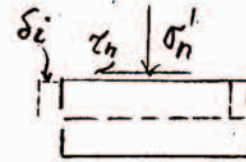
#### 1) In a Material Property

- Same value whether test undist. vs remolded or NC vs OC
- Little effect of strain rate (unless very fast)
- But must shear sufficiently to obtain max. particle orientation. ∴ Plot  $\tau/\sigma'_n$  vs  $\log \delta$  (displacement)



#### 2) Testing methods

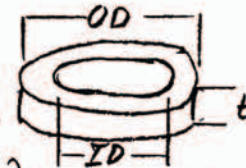
- a) Repeated direct shear, i.e. shear to  $\delta_i$ , push back, shear again, etc



- Either precut natural (to greatly reduce  $\delta$ )
  - Or remold & consolidate on plate (MSD ...)
- } Both used

- b) Rotational shear = ring shear

| OD   | ID   | t (cm) |   |
|------|------|--------|---|
| 7.1  | 5.1  | 0.4 ±  | Harvard (La Gatta 1970)                                 |
| 15.2 | 10.2 | 1.9    | Imperial College & NEI                                  |
| 10   | 7    | 0.5    | Stark & Eid (1993), UofI (Modified Bromhead ring shear) |



Best procedure → minimum envelope

Typical  $d\delta/dt \approx \dot{\delta} \approx 1 \text{ cm/day}$

#### 3) Some results

- See Fig 14 below → same result for precut vs intact (needed much larger  $\delta$ )
- Also note reducing  $\tau_r/\sigma'_n$  with increasing  $\sigma'_n \approx$  curved envelope

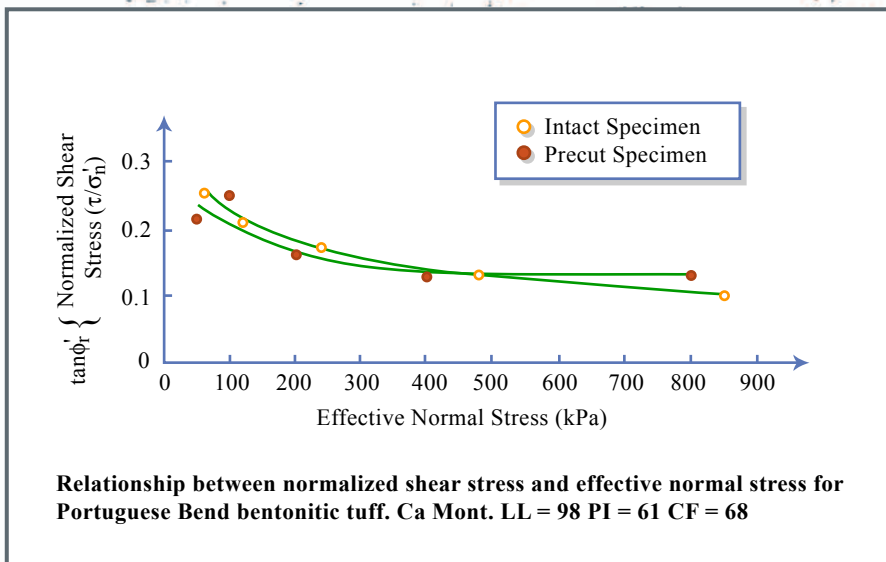
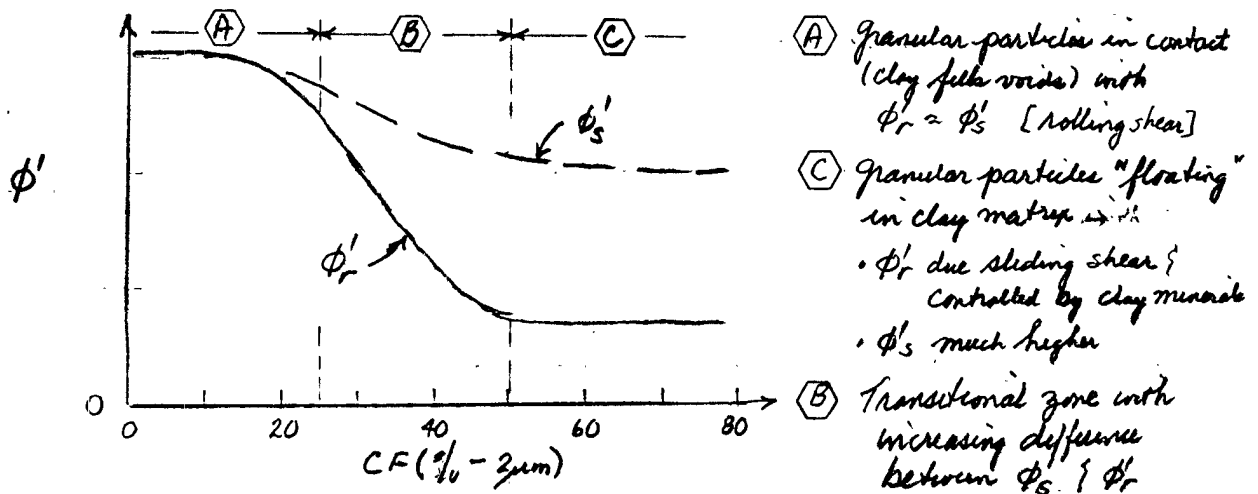


Figure by MIT OCW. Adapted from: Stark & Eid (1993) GTJ, ASTM 16(1)



### 1.4 Overview of Softened (Critical State) and Residual $\phi'$

Lupini et al. [1981, Geot 13(1)] Skempton [1985, Geot. 35(1)]



### 1.5 Recommended Selection of $c'$ & $\phi'$ Until Approx. Mid-1990s

(Mostly by Skempton, e.g. 1970 [Geot 20(3)] & 1977 [9th ICSMFE, Vol 3])

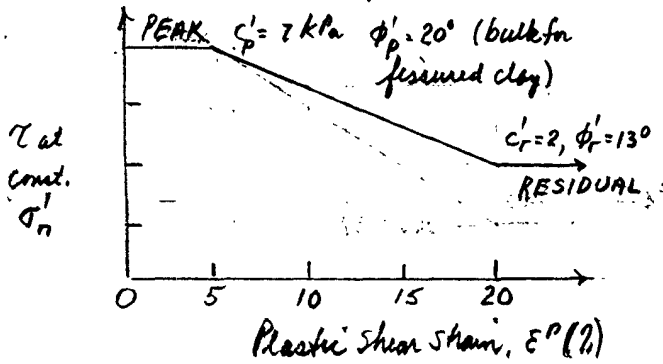
- 1) Along PRIOR FAILURE SURFACE having movements of  $\approx 1-2m$   
Must use  $\phi_r$  independent of age of prior failure
  - CD DS tests on block sample from 10<sup>6</sup> yr. old failure at Mangla Dam  $\rightarrow \tau_{max} = \sigma'_n \tan \phi_r$
- 2) 1<sup>st</sup> time failure, HOMOGENEOUS CLAY (no fissures or stratification, etc.)  
Can use  $c'_p$  &  $\phi'_p$  (CCL NOTE: Only if shearing does not  $\rightarrow$  strain softening after peak, which is not likely for OC clay)
- 3) 1<sup>st</sup> time failure, FISSURED CLAYS
  - For London clay, use  $c'=0$  &  $\phi' = \phi'_s$ , i.e. softening of fissures due to swelling and localized straining  $\rightarrow$  fully softened condition (empirical observation from back analysis of case histories)
  - For some fissured clays, may get  $\phi' < \phi'_s$ ,

e.g. Stark & Eid [1997, JGGE 123(4)] - Analysis of 14 failures involving stiff fissured clays  $\rightarrow \tau_m = \frac{1}{2}(\tau_s + \tau_r)$  for LL > 60%, i.e. half way between fully softened & residual)



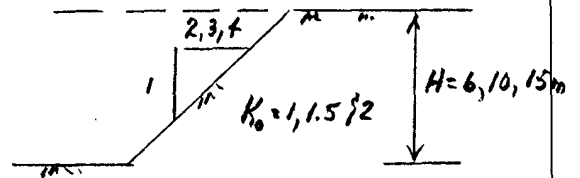
1.6 Results of Research by Potts et al. (1997) "Delayed collapse of cut slopes in stiff clay" Geot 47(5), 953-982

1) Conducted coupled FE analyses (i.e. included  $k$ ) of cut slopes on a strain softening clay (patterned after London clay)



Boundary Conditions

\* Surface suction = 10 kPa

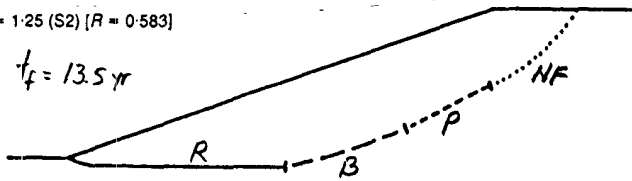


Note: Also did analyses without strain softening  $\rightarrow$  longer  $t_f$  and higher  $\bar{\tau}_u = \text{average } \tau_u = u/\sigma_v$  on rupture surface. Incr. suction also  $\rightarrow$  much longer  $t_f$  (i.e. vegetation on slope helps)

2) Results for  $H=10\text{m}$ , 1V:3H as  $f(K_0)$  : Collapse = failure when analyses showed abrupt increase in  $S_h$  at mid-slope

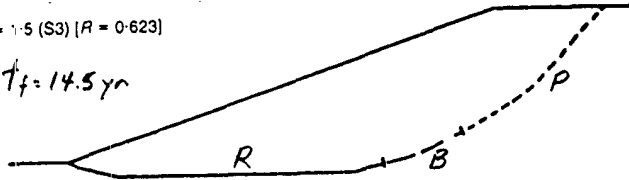
$K_0 = 1.25$  (S2) ( $R = 0.583$ )

$t_f = 13.5 \text{ yr}$



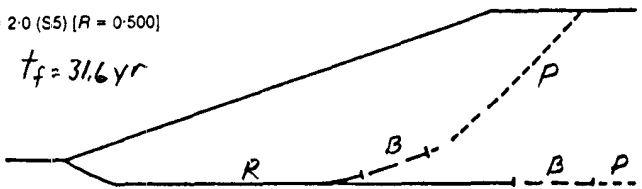
$K_0 = 1.5$  (S3) ( $R = 0.623$ )

$t_f = 14.5 \text{ yr}$



$K_0 = 2.0$  (S5) ( $R = 0.500$ )

$t_f = 31.6 \text{ yr}$



- NF ..... Rupture surface not formed
- P - - - - - Rupture surface at peak
- B - - - - - Rupture surface between peak and residual
- R - - - - - Rupture surface at residual

$$R = \frac{\bar{\tau}_p - \bar{\tau}}{\bar{\tau}_p - \bar{\tau}_r}$$

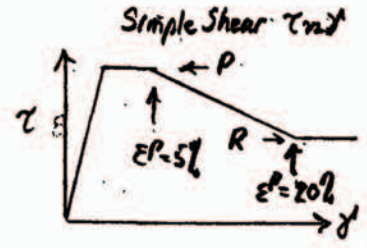
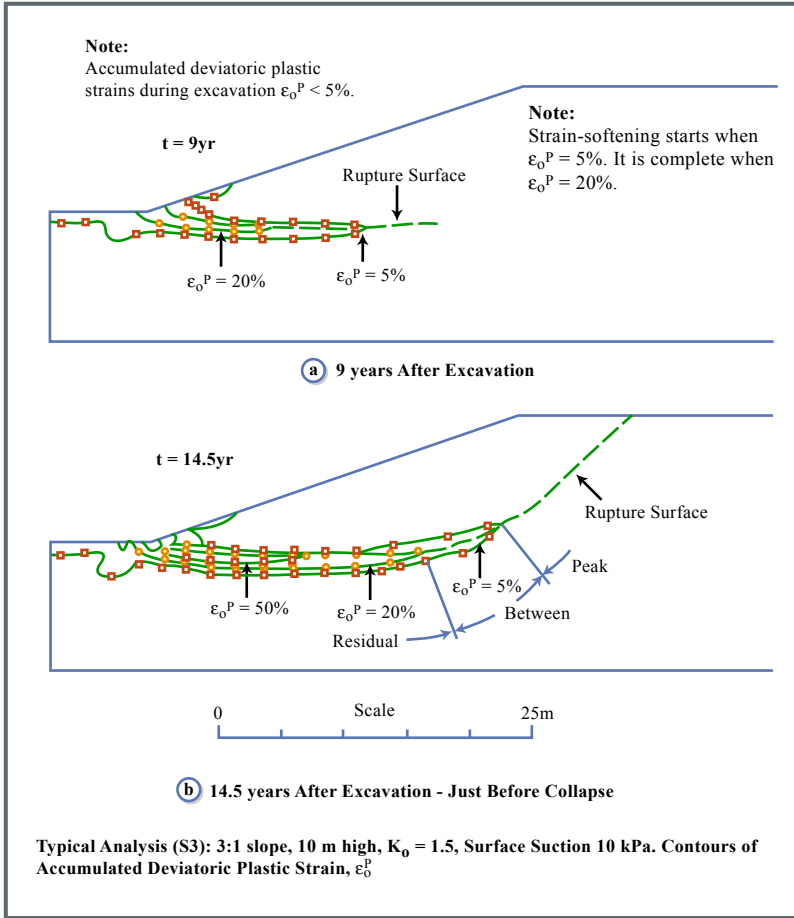
These results show that % of slope at residual (R), at peak (P), inbetween (B) and not even at failure (NF) varies as  $f(K_0)$ .  
Varying slope height and angle also  $\rightarrow$  varying percentages

$\therefore$  No single envelope at failure

Fig. 21. Rupture surfaces predicted by the analyses on 3:1 slopes, 10 m high, with surface suction 10 kPa and varying  $K_0$



3) Results showing strain contours for  $H=10m$ ,  $V:3H$  and  $K_0=1.5$   
 at  $t=9yr$  }  $t=t_f=14.5yr$

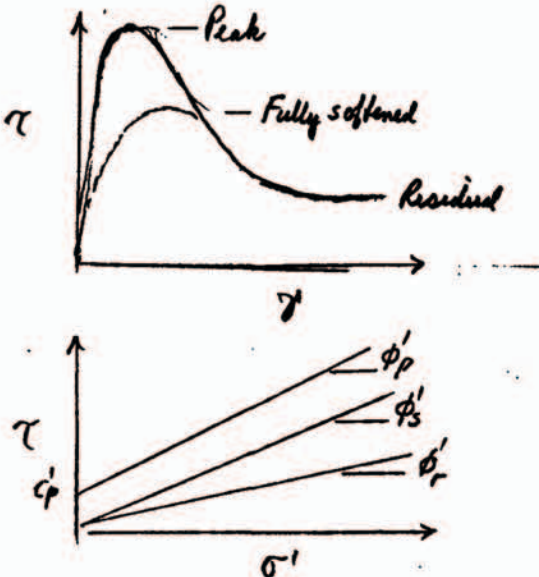


No. 5505  
 Engineer's Computation Pad



Figure by MIT OCW.

4) Conclusions



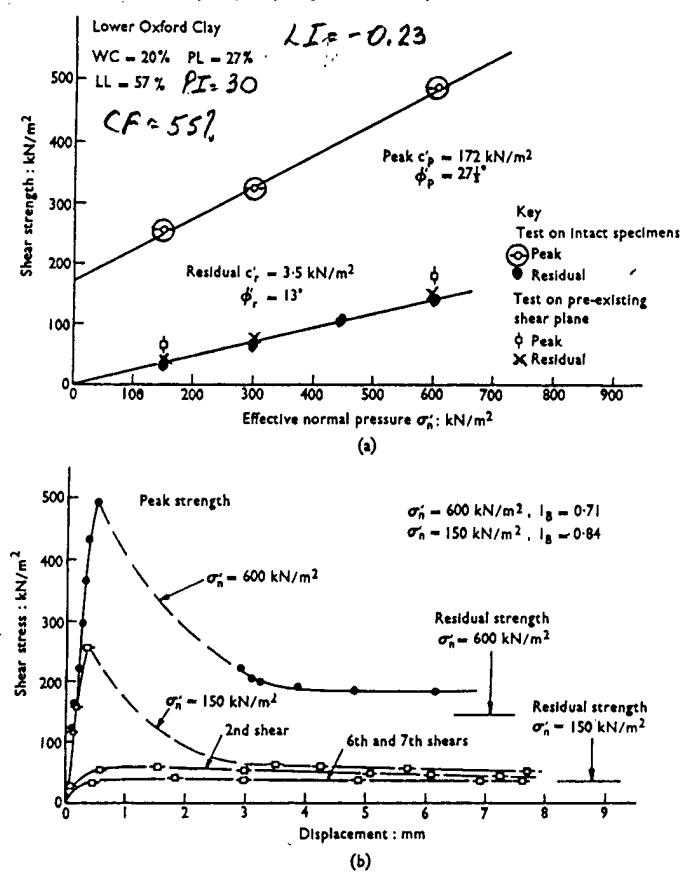
- Drained shear of all OC clays in slopes will undergo strain softening
- Increased degree of strain softening from peak to fully softened (NC) to residual will decrease  $t_f$  (less pore pressure dissipation and swelling  $\rightarrow$  failure)
- Get progressive failure mechanism starting at toe and moving upslope
- No single envelope at failure

1.7 Mesri et al. (SOA paper submitted to JGGE, 3/00)

- 1) Analysis of  $\approx 100$  case histories of failures (1<sup>st</sup> time & reactivated)
- 2) Principal conclusions
  - a) Most stiff clays & clay shales are NOT homogeneous. Rather usually stratified (bedding planes, laminations, etc.) and/or fissured
  - b) Stratified layers often more plastic and weaker and require less displacement to reach residual condition; may even be at residual before excavation or due to unchained shear during excavation.
  - c) In many cases, stratification often leads to formation of near horizontal failure surface at residual condition
  - d) Suggests using (I think based on Fig 17 ICT)
    - Fully softened envelope along inclined failure surface
    - Residual " " horizontal " "

No. 5505 Engineer's Computation Pad

Burland et al. (1977) *geot.* 27(4), 557-591  
Strongly laminated cemented (10-20% CaCO<sub>3</sub>) and fissured clay shale



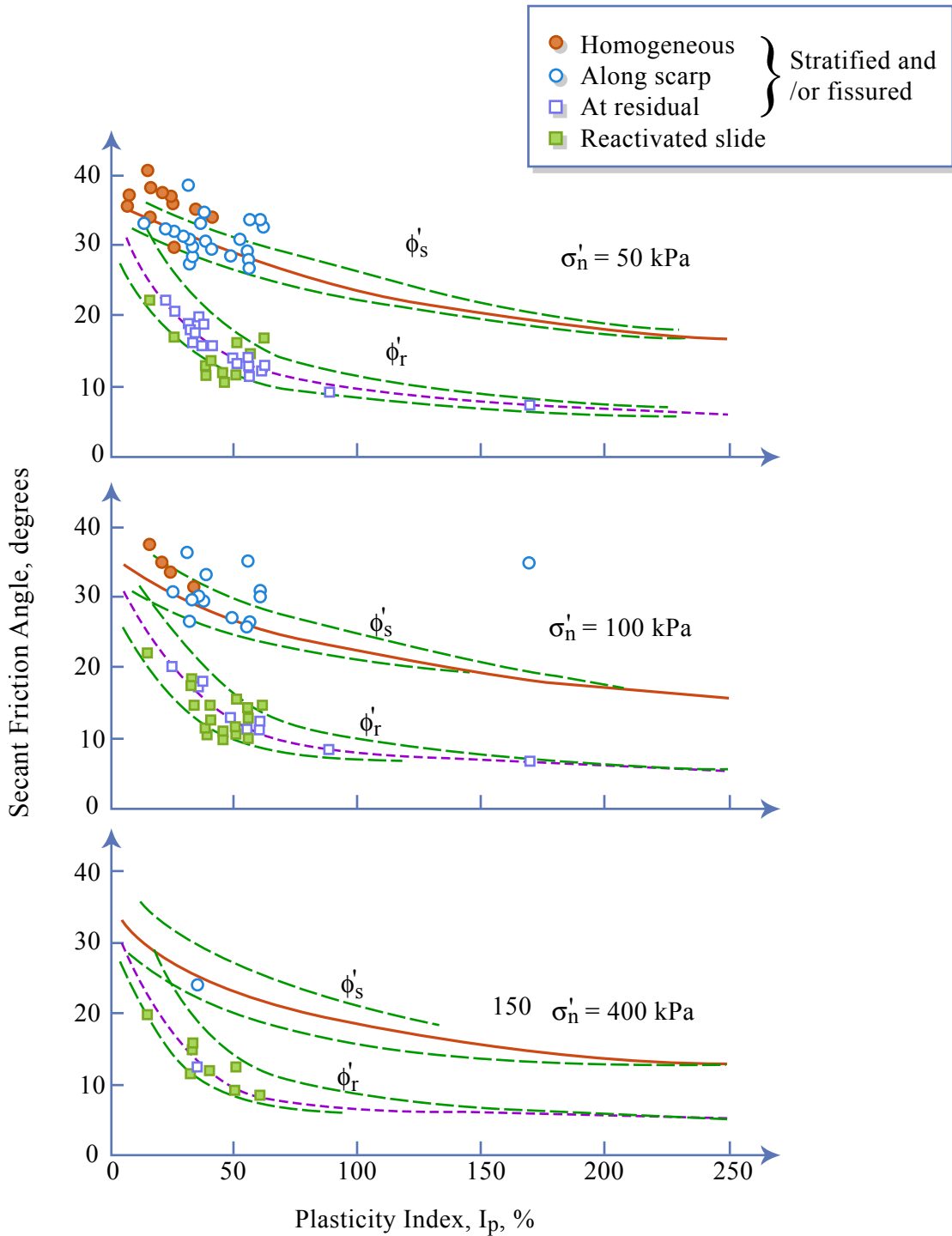
Example of large difference between peak & residual envelopes along bedding plane

Fig. 5. Typical shear stress-displacement curves and strength envelope for direct drained shear tests on Lower Oxford Clay specimens sheared parallel to the bedding

1.7 Cont.

CCL 4/3/01

No. 5505  
Engineer's Computation Pad



Mobilized friction angles back-calculated from reactivated and first-time slope failures compared to the range from empirical information.

Figure by MIT OCW.

Adapted from: Mesri & Shahien (2/00) DO NOT REPRODUCE

4/90 4/96 3/98 4/3/01

1.8 Basic Research on  $\phi'_r$  Kenney (1967) Olsow Conf; (1977) ICJMFGE

| Mineral      | %-2 $\mu$ | % Salt | $w_p$ (%) | $I_p$ (%) | $\phi'_r$ (tan $\phi'_r$ ) |
|--------------|-----------|--------|-----------|-----------|----------------------------|
| Quartz       | 100       | -      | -         | 0         | 35 (0.70)                  |
| Al Hapulgite | 74        | -      | 345       | 240       | 29.6 (0.57)                |
| Na Illite    | 100       | 0      | 51        | 18        | 16.2 (0.29)                |
|              |           | 30     | 99        | —         | ( )                        |
| Na. Mont.    | 100       | 0      | 1325      | 1270      | 4.0 (0.07)                 |
|              |           | 30     | 620       | —         | ( )                        |

Mixtures of massive & clay minerals\*

$$R_{\phi_r} = \frac{\tan \phi'_r (\text{Mixture}) - \tan \phi'_r (\text{Clay})}{\tan \phi'_r (\text{Massive}) - \tan \phi'_r (\text{Clay})}$$

\* See IC9

1.9 Empirical Correlations

- Voight (1973) geot 23(2)
- Lupini et al (1981) geot 31(2) + fundamental studies - See IC10
- Deere  $\phi'_r \sim I_p$  IC10
- Stark & Eid (1994) JG&E, ASCE, 120(5) IC11

|          |  |  |
|----------|--|--|
| CF < 25% | Low $I_p$ : Relatively little particle reorientation                                 | CCL<br>Higher $\bar{\sigma}_{vm} / \bar{\sigma}$ |
| CF > 50% | High $I_p$ : Significant particle reorientation<br>(Can get highly polished surface) | Lower $\bar{\sigma}_{vm} / \bar{\sigma}$         |

Skempton (1985)  
geot 35(1)

Residual Friction Angle of Soils

Kenney (1977) "Residual Strength of Mineral Mixtures"

9th ICSMFE Vol.1 pp. 155-160

Results from repeated Direct Shear at  $\sigma'_n = 1 \text{ kg/cm}^2$

$$R_{\phi}' = \frac{\tan \phi'_r (\text{Mixture}) - \tan \phi'_r (\text{Clay})}{\tan \phi'_r (\text{Massive}) - \tan \phi'_r (\text{Clay})}$$

TABLE II. RESULTS OF RESIDUAL STRENGTH TESTS ON MIXTURES.

| Mixture  | Salinity gm/l | * Mineral Content % dry wt. |                          | Residual State $\sigma'_n = 1.0 \text{ kg/cm}^2$ |                         |                    |
|--|---------------|-----------------------------|--------------------------|--|-------------------------|--------------------|
|  |               | Mixture % dry weight        | Total Massive Total Clay | $w_{res}$ %                                      | % Volume Clay and Water | $\tan \phi'_{res}$ |
| <b>A. MIXTURES CONTAINING MONTMORILLONITE</b>        |               |                             |                          |  |                         |                    |
| Montmorillonite - Na and Quartz                      | 0             | 60/50                       | 60 50                    | 200  | 92                      | 0.09               |
|  |               | 25/75                       | 25 75                    | 96   | 80                      | 0.11               |
|  |               | 10/90                       | 10 90                    | 44   | 60                      | 0.42               |
|  |               | 5/95                        | 5 95                     | 39   | 54                      | 0.61               |
| Montmorillonite - Na and Quartz                      | 30            | 50/50                       | 50 50                    | 72   | 84                      | 0.24               |
|  |               | 25/75                       | 25 75                    | 51   | 69                      | 0.38               |
|  |               | 10/90                       | 10 90                    | 34   | 54                      | 0.56               |
| Montmorillonite - Na and Amorphous SiO <sub>2</sub>  | 30            | 50/50                       | 50 50                    | 150  | 90                      | 0.21               |
|  |               | 25/75                       | 25 75                    | 87   | 78                      | 0.24               |
| Bentonite and Quartz                                 | 0             | 75/25                       | 44 56                    | 61   | 84                      | 0.12               |
|  |               | 50/50                       | 62 38                    | 52   | 75                      | 0.25               |
|  |               | 25/75                       | 81 19                    | 42   | 63                      | 0.40               |
|  |               | 15/85                       | 89 11                    | 32   | 53                      | 0.64               |
| Bentonite and Amorphous SiO <sub>2</sub>             | 0             | 91/9                        | 32 68                    | 70   | 89                      | 0.10               |
|  |               | 82/18                       | 39 61                    | 56   | 84                      | 0.11               |
|  |               | 68/32                       | 49 51                    | 68   | 81                      | 0.13               |
|  |               | 47/53                       | 65 35                    | 60   | 76                      | 0.18               |
|  |               | 25/75                       | 81 19                    | 47   | 66                      | 0.27               |
|  | 10/90         | 92 8                        | 51                       | 61   | 0.49                    |                    |
| <b>B. MIXTURES CONTAINING KAOLINITE AND GRUNDITE</b> |               |                             |                          |  |                         |                    |
| Kaolinite and Quartz                                 | 0             | 75/25                       | 25 75                    | 40   | 88                      | 0.32               |
|  |               | 60/50                       | 50 50                    | 30   | 73                      | 0.49               |
|  |               | 25/75                       | 75 25                    | 23   | 54                      | 0.65               |
| Kaolinite and Amorphous SiO <sub>2</sub>             | 0             | 75/25                       | 25 75                    | 44   | 89                      | 0.32               |
|  |               | 50/50                       | 50 50                    | 31   | 74                      | 0.41               |
| Grundite - Na and Quartz                             | 0             | 75/25                       | 25 75                    | 67   | 91                      | 0.25               |
|  |               | 50/50                       | 50 50                    | 49   | 79                      | 0.40               |
| Grundite - Na and Quartz                             | 30            | 75/25                       | 25 75                    | 63   | 91                      | 0.22               |
|  |               | 50/50                       | 50 50                    | 40   | 77                      | 0.40               |
|  |               | 25/75                       | 75 25                    | 36   | 62                      | 0.62               |
| <b>C. MIXTURES CONTAINING HYDROUS MICA</b>           |               |                             |                          |  |                         |                    |
| Hydrous mica I - Na and Quartz                       | 0             | 75/25                       | 48 52                    | 30   | 74                      | 0.35               |
|  |               | 60/50                       | 65 35                    | 31   | 65                      | 0.44               |
| Hydrous mica I - Na and Quartz                       | 30            | 75/25                       | 48 52                    | 32   | 75                      | 0.38               |
|  |               | 60/50                       | 65 35                    | 33   | 66                      | 0.46               |
| Hydrous mica I - K and Quartz                        | 0             | 75/25                       | 48 52                    | 30   | 74                      | 0.41               |
|  |               | 50/50                       | 65 35                    | 30   | 65                      | 0.47               |
| Hydrous mica I - K and Quartz                        | 30            | 75/25                       | 48 52                    | 41   | 78                      | 0.49               |
|  |               | 50/50                       | 65 35                    | 35   | 67                      | 0.50               |
| Hydrous mica II - Na                                 | 0             | 75/25                       | 33 67                    | 31   | 80                      | 0.32               |
|  |               | 60/50                       | 55 45                    | 22   | 66                      | 0.46               |
| Hydrous mica II - Na                                 | 30            | 75/25                       | 33 67                    | 41   | 83                      | 0.45               |
|  |               | 60/50                       | 55 45                    | 27   | 67                      | 0.47               |
| Hydrous mica III - Na                                | 0             | 75/25                       | 33 67                    | 54   | 85                      | 0.44               |
|  |               | 60/50                       | 55 45                    | 40   | 74                      | 0.48               |
| Hydrous mica III - Na                                | 30            | 75/25                       | 33 67                    | 52   | 85                      | 0.44               |
|  |               | 60/50                       | 55 45                    | 46   | 76                      | 0.50               |

\* Thick massive-clay % are reversed

"Low Clay"



"High Clay"



Sand particles inhibit reorientation of clay particles

$\eta = 60\% \rightarrow e = 1.5$

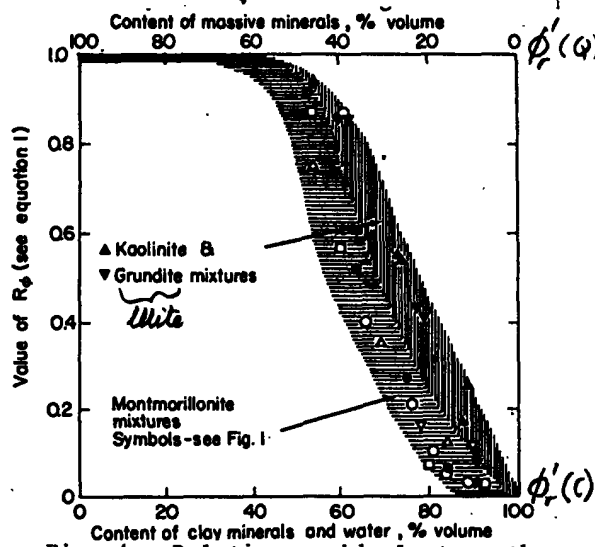


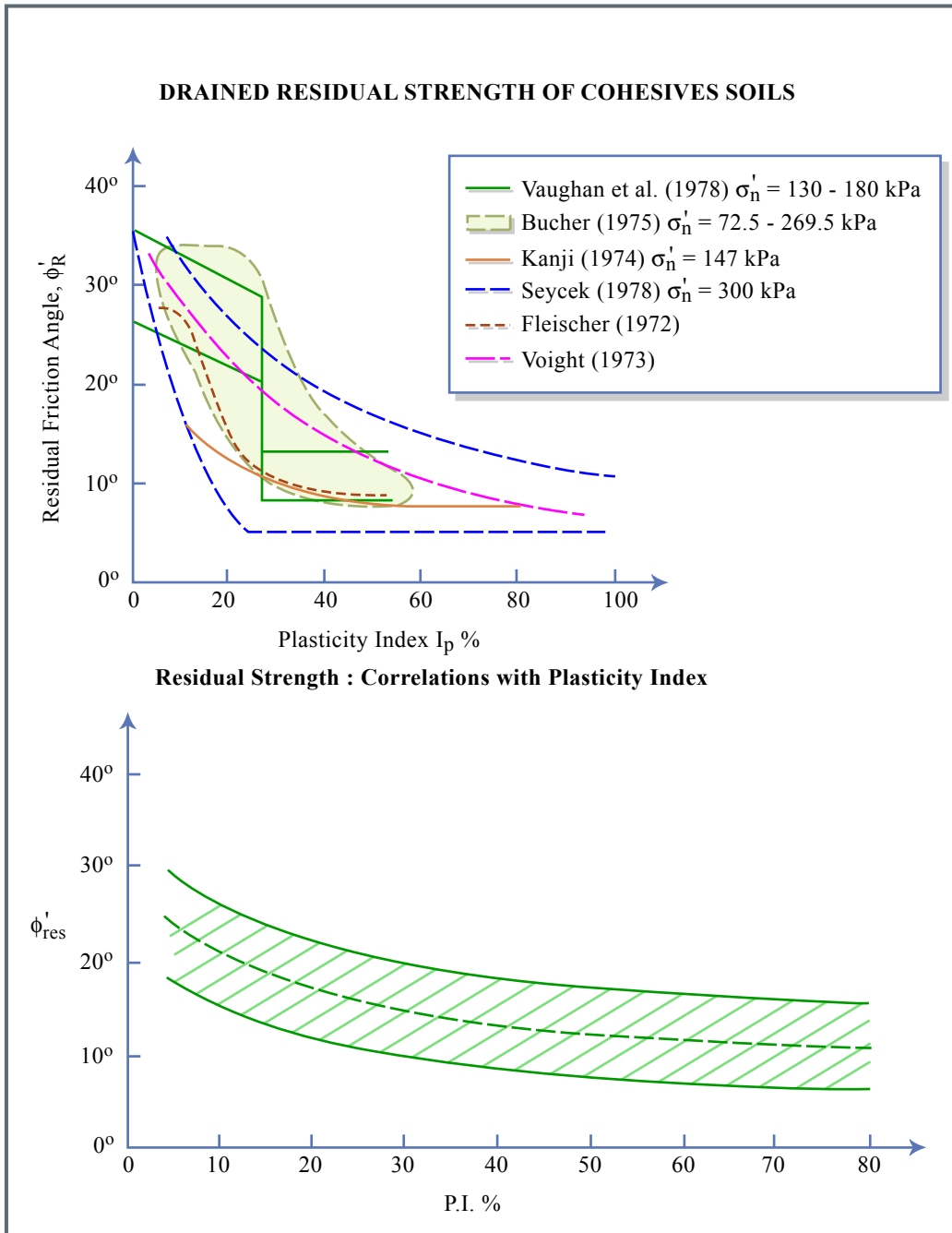
Fig. 4. Relative residual strength

CCL 4/2/87 1.322

4/89 4/3/01  
1.9(2x2) Empirical Correlations :  $\phi'_r$  (See IC7 for  $\phi'_s$ )

IC7

Lupini, Skinner & Vaughan (1981) Geotechnique V31 No.2, pp 181-20  
(Contains alot of fundamental research on topic)

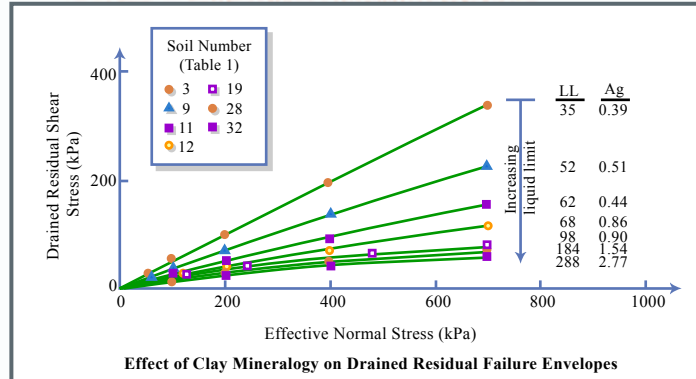


CC Ladd  
4/74

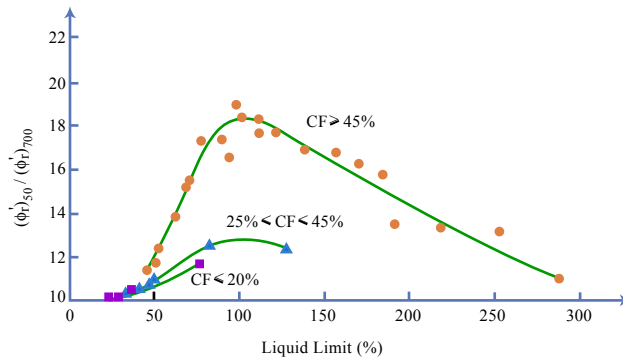
Figure by MIT OCW.

**DRAINED RESIDUAL STRENGTH OF COHESIVE SOILS**

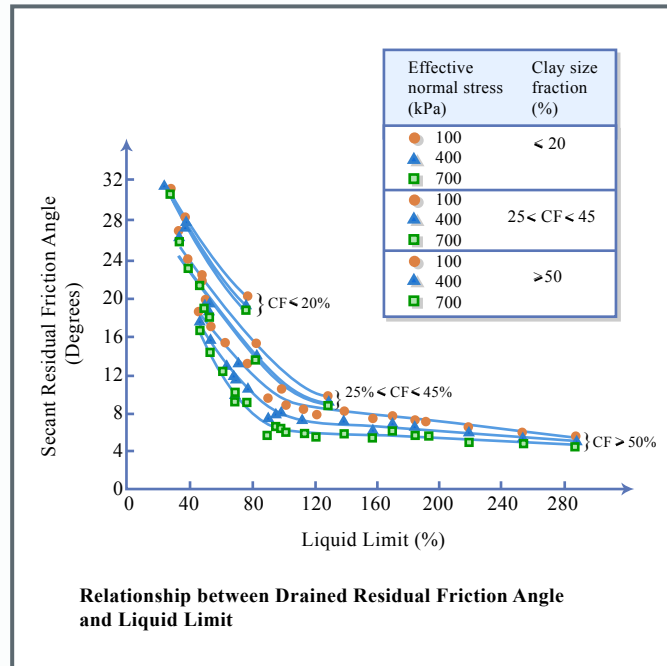
By Timothy D. Stark,<sup>1</sup> Associate Member, ASCE,  
and Hisham T. Eid,<sup>2</sup> Student Member, ASCE



Effect of Clay Mineralogy on Drained Residual Failure Envelopes



Reduction in Secant Residual Friction Angle from Effective Normal Stresses of 50 kPa to 700 kPa



Relationship between Drained Residual Friction Angle and Liquid Limit

Figures by MIT OCW  
Adapted from:

JGF, ASCE 120(5) (1994)

Results of torsional ring shear tests on 32 clays and shales → empirical correlation of  $\phi'_r$  as function  $w_L$ , CF (%-3 $\mu$ m) and  $\sigma'_n$ . Tests on remolded specimens = mixture distilled H<sub>2</sub>O with air-dried soil after ball-milling to obtain 100% - #200 sieve (to break down aggregates).

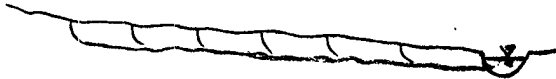
**NOTE: Ball-milling essential to breakdown air-dried aggregates → correct AI/CF**

50 SHEETS  
100 SHEETS  
200 SHEETS  
22-141  
22-142  
22-144  
AMPS



C2, HIGHLY STRUCTURED, SENSITIVE CLAYS (Quick Clays)

2.1 Background



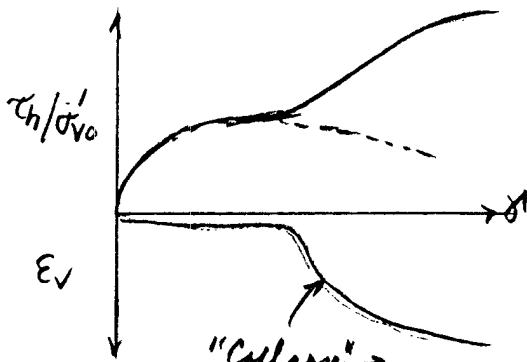
Flake and/or retrogressive

- Almost flat slope (Norway)
- "Mini"  $\Delta$  geometry  $\rightarrow$  massive flow slide
  - Putney 3<sup>rd</sup> floor
  - Rissa film

• Approach = f(location)

2.2 Norway Aas (1981) ICSMFE

- Analysis 5 "flake" type slides: Treats as CU Case via USA



— CK<sub>0</sub>D/DSS  
--- CK<sub>0</sub>U/DSS

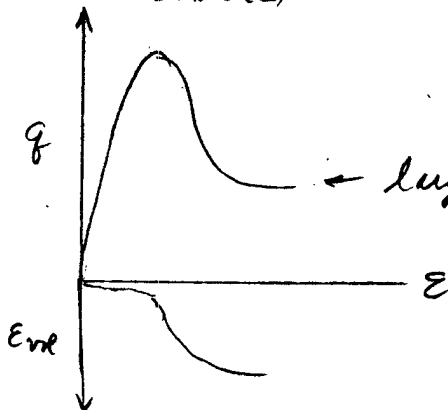
In situ  $\tau/\sigma'_{v0} = 0.18 \pm 0.035$

Lab CK<sub>0</sub>U/DSS  $c_u/\sigma'_{v0} = 0.195 \pm 0.025$

"Collapse"  $\rightarrow$   
Undrained condition:  $u_{sh} > 0$

2.3 Quebec Lefebvre (1981) CGJ p420

- Treats as CD Case using equilibrium  $u$ , but "large strain" values of  $c'$  &  $\phi'$



CIDC(L)

large strain ( $\epsilon \approx 10\%$ ) used to select  $c'$  &  $\phi'$

See ICB

CCL: Seems more empirical than 2.2, but applied to circular arc type failures

SLOPE STABILITY-QUICK CLAYS  
(Canada)

IC13

SEBJ NBR 1983

CCL 1.322 4/84 4/88

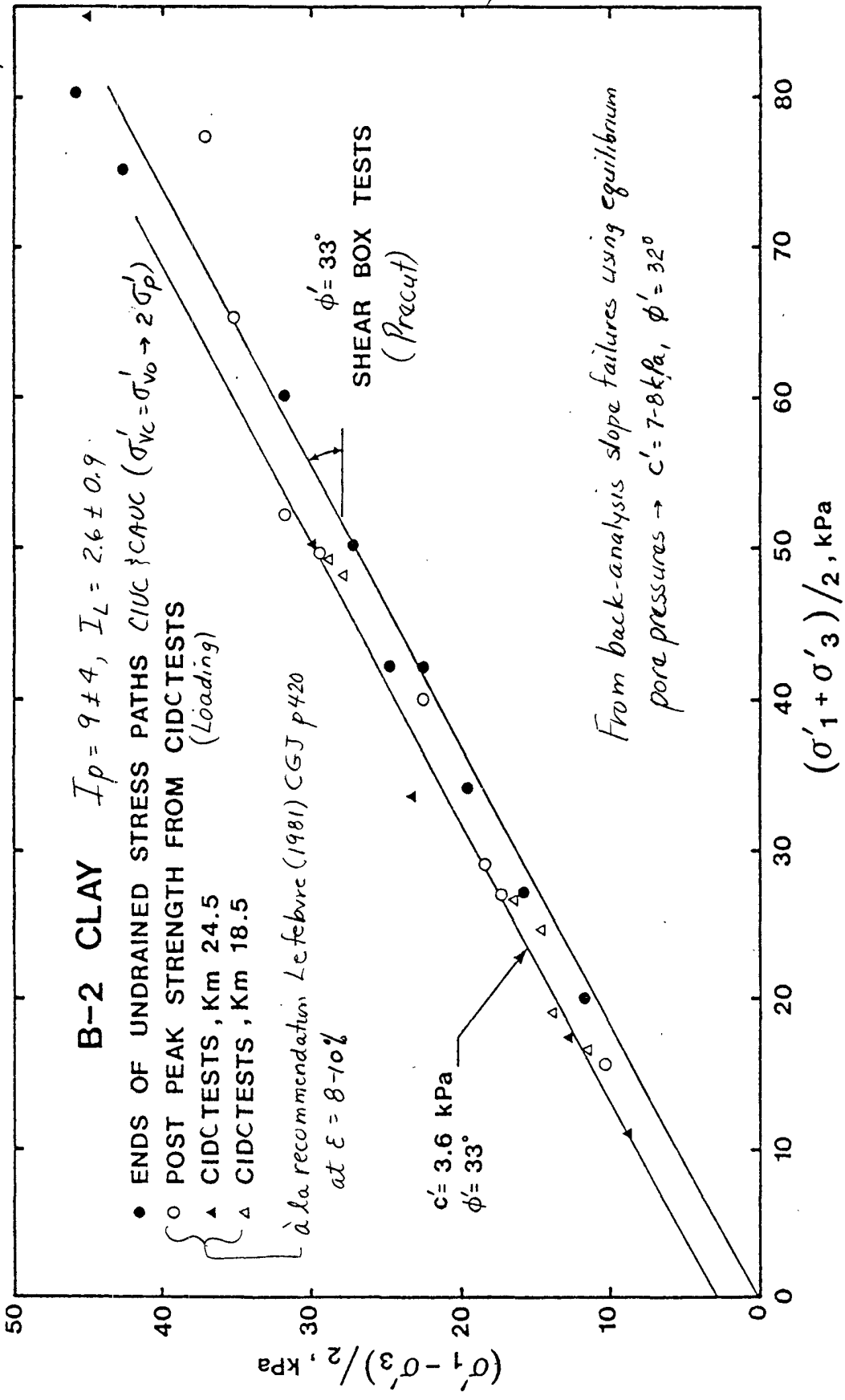


FIG. 5.5-9 TYPICAL EFFECTIVE STRENGTH ENVELOPES B-2

From SEBJ (not for publication)

CCL 4/17/85

1.322

SLOPE STABILITY

ICM

4/89 4/90 4/96 +101

### C3. Effective Stress Envelopes for Conn. Valley Varved Clay

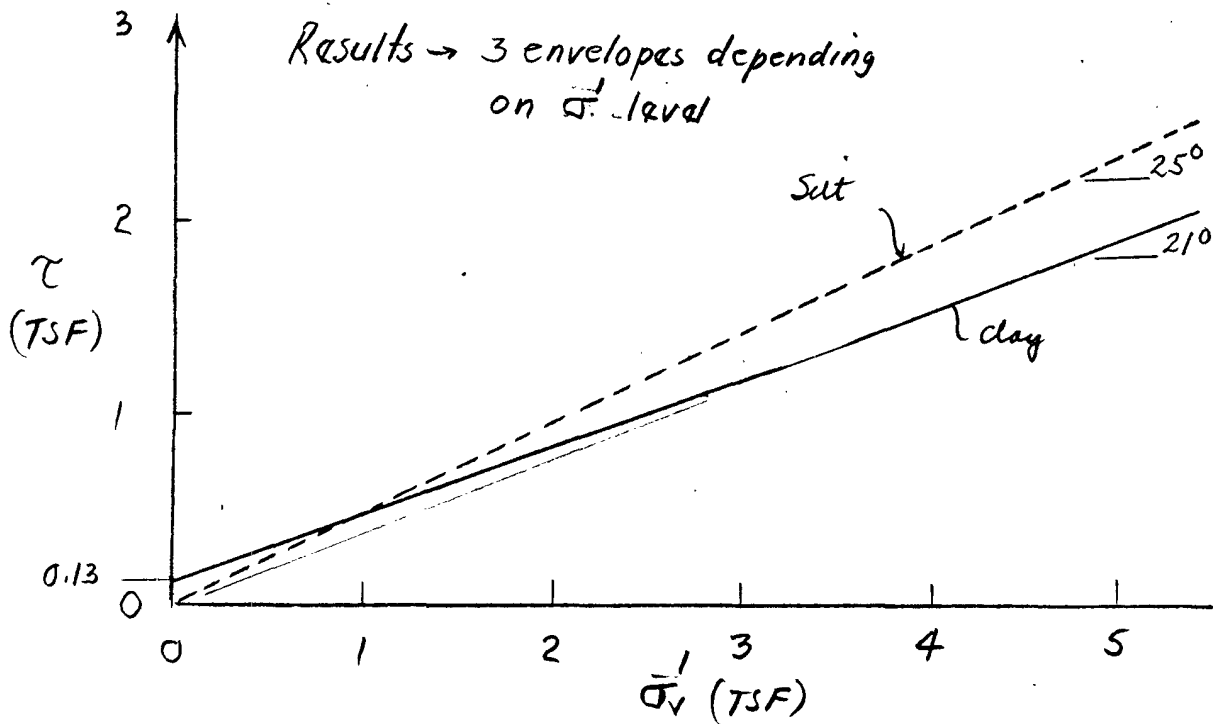
Ladd (1975) MIT Report

Ladd & Foott (1977) FHWA Report

a) CDSS Parallel to Varves (Clay w/  $\sigma'_p \approx 3.5$  TSF)

----- Shear through "silt" layer

———— Shear " " "clay" layer



b) Summary of ESE Data

Bulk  $I_p = 15-30\%$

Ladd & Foott (1977) FHWA

CU Shear Across Varves

Compression & Extension  
SHANSEP Tests

$c'/\sigma'_{vm} = 0.012$   $\phi' = 30^\circ$

CD Shear In Clay Varves

$c'/\sigma'_p = 0.025$   $\phi' = 20^\circ$