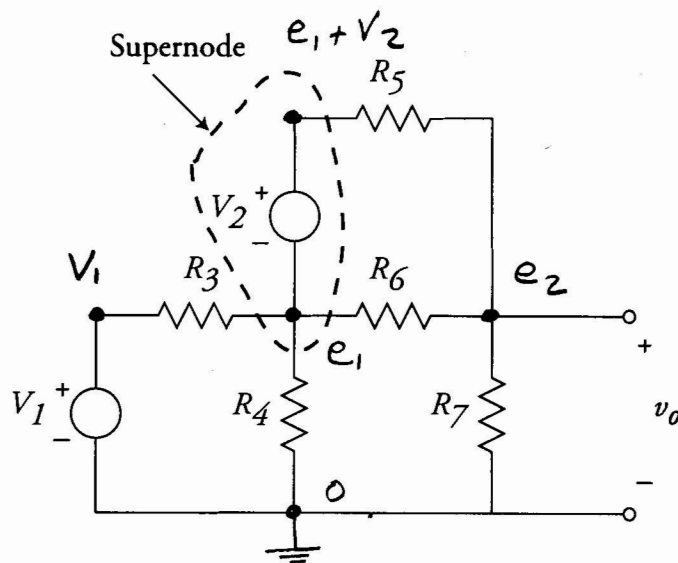


The nodes are labeled as below:



Note that 4 of the nodes (ground, v_1 , e_1 , e_2) are labeled normally. The 5th node is labeled as $e_1 + V_2$, not e_3 , since there is a known potential difference across V_2 .

To start, apply KCL at e_2 :

$$e_2: \frac{e_2 - 0}{R_7} + \frac{e_2 - e_1}{R_6} + \frac{e_2 - (e_1 + V_2)}{R_5} = 0$$

$$\Rightarrow -\left(\frac{1}{R_5} + \frac{1}{R_6}\right)e_1 + \left(\frac{1}{R_5} + \frac{1}{R_6} + \frac{1}{R_7}\right)e_2 = \frac{V_2}{R_5}$$

This result is typical of the node method in simpler problems.

Next, apply KCL at nodes e_1 and $e_1 + V_2$:

$$e_1: \frac{e_1 - V_1}{R_3} + \frac{e_1 - 0}{R_4} + \frac{e_1 - e_2}{R_6} - i_2 = 0$$

$$e_1 + V_2: \frac{e_1 + V_2 - e_2}{R_5} + i_2 = 0$$

Note that the constitutive law for the V_2 source gives no information about i_2 . However, we can eliminate i_2 by adding the two equations above:

$$\begin{aligned} \text{supernode: } & \left(\frac{1}{R_3} + \frac{1}{R_4} + \frac{1}{R_5} + \frac{1}{R_6} \right) e_1 - \left(\frac{1}{R_5} + \frac{1}{R_6} \right) e_2 \\ & = \frac{1}{R_3} V_1 - \frac{1}{R_5} V_2 \end{aligned}$$

Plugging in values, we have

$$\begin{aligned} 2.5 e_1 - e_2 &= 2.5 \\ -e_1 + 2e_2 &= 2.5 \end{aligned}$$

Solving for e_1, e_2 , we have

$$e_1 = 1.875 \text{ V} \quad e_2 = 2.1875 \text{ V}$$

Since $v_o = e_2 - 0$,

$$v_o = 2.1875 \text{ V}$$